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# Mark Scheme (Results)

January 2020

Pearson Edexcel International GCSE In Mathematics A (4MA1) Paper 2H

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## **General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded.
   Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme.
  - Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

## Types of mark

o M marks: method marks

o A marks: accuracy marks

B marks: unconditional accuracy marks (independent of M marks)

#### Abbreviations

- o cao correct answer only
- o ft follow through
- o isw ignore subsequent working
- o SC special case
- o oe or equivalent (and appropriate)
- o dep dependent

- o indep independent
- o awrt answer which rounds to
- eeoo each error or omission

### No working

If no working is shown then correct answers normally score full marks If no working is shown then incorrect (even though nearly correct) answers score no marks.

## With working

If there is a wrong answer indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.

If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.

If a candidate misreads a number from the question. Eg. Uses 252 instead of 255; method marks may be awarded provided the question has not been simplified. Examiners should send any instance of a suspected misread to review. If there is a choice of methods shown, mark the method that leads to the answer on the answer line; where no answer is given on the answer line, award the lowest mark from the methods shown.

If there is no answer on the answer line then check the working for an obvious answer.

## • Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.

Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

## Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded to another. **International GCSE Maths** 

Apart from Questions 3, 7b, 12, 17, 20, 22 the correct answer, unless clearly obtained by an incorrect method, should be taken to

imply a correct method

	Q	Working	Answer	Mark	Notes
1	(a)		$x^7$	1	B1
	(b)	eg $7^8 \times 7^4 = 7^{12}$ or $7^8 \div 7^3 = 7^5$ or $7^5 \times 7^4$ or $7^4 \div 7^3 = 7$ or $7^8 \times 7$ or $7^{12} \div 7^3 = 7^{12} \div 3$		2	M1 for one correct step – must be written as a power of 7
			79		A1 for 7 <sup>9</sup>
					Total 3 marks

2	$32.4 \times 100^3$		2	M1	for $32.4 \times 100^3$ oe
		32 400 000		A1	for 32 400 000 accept $3.24 \times 10^7$
					Total 2 marks

3	$\frac{14}{3}(+)\frac{19}{5}$ or $(4)\frac{10}{15}(+)(3)\frac{12}{15}$ or $(4)\frac{10a}{15a}(+)(3)\frac{12a}{15a}$		3	M1	for correct improper fractions or fractional part of numbers written correctly over a common denominator
	$eg \frac{14 \times 5 + 19 \times 3}{3 \times 5} \text{ or } \frac{70}{15} + \frac{57}{15} \text{ or } \frac{70a}{15a} + \frac{57a}{15a} \text{ or}$ $4\frac{10}{15} + 3\frac{12}{15} = 7\frac{22}{15} \text{ oe}$			M1	for correct fractions with a common denominator of 15 or a multiple of 15
	$\frac{70}{15} + \frac{57}{15} = \frac{127}{15} = 8\frac{7}{15} \text{ or } 7\frac{22}{15} = 8\frac{7}{15}$ or if shows $8\frac{7}{15} = \frac{127}{15}$ at the beginning then show that the addition comes to $\frac{127}{15}$	Shown		A1	dep on M2 for a correct answer from fully correct working <b>or</b> shows that  RHS = $\frac{127}{15}$ <b>and</b> fully correct working shows LHS = $\frac{127}{15}$
					Total 3 marks

4	30 + 4x + 10 + x + 20 = 5x + 60 or $180 - 30 = 150$		4	M1	Allow $5x + 60 = n$	M2 for
					where $n \neq 180$ or for	5x + 30 = 150
					subtracting 30 from 180	oe
	e.g. $30 + 4x + 10 + x + 20 = 180$ or $5x + 60 = 180$ oe			M1	for setting up the	
					equation or for	
	or 180 – 30 – 10 – 20 (=120)				subtracting all	
					numerical values of	
					angles from 180	
	5x = 120 or $20$ ÷ 5			M1	for correctly simplifying	to $ax = b$ or for
					dividing '120' by 5	
		24		A1	for 24	
						Total 4 marks

5	Fully correct angle	2	B2	Fully correct angle bisector with all
	bisector with all			arcs shown.
	relevant arcs			B1 for all arcs and no angle bisector
	shown			drawn or for a correct angle bisector
				within guidelines but not arcs or
				insufficient arcs
				Total 2 marks

6	1 - (0.24 + 0.31) (= 0.45)		4	M1	or for a correct equation for
	Or				missing values eg
	$(0.24 + 0.31) \times 180 (= 99)$				x + 0.24 + 2x + 0.31 = 1 oe
					(can be implied by 2 probabilities
					that total 0.45 in table if not
					contradicted in working space)
	'0.45' ÷ 3 (= 0.15)			M1	(or 0.15 correctly placed in table
	Or				as long as not contradicted)
	'0.45' × 180 (= 81)				,
	Or				
	180 - 99 (= 81)				
	'0.15' × 180			M1	s 27
	Or				or for an answer of $\frac{27}{180}$
	'81' ÷ 3				100
		27		A1	
					Total 4 marks

7	(a)	2x > 4 - 7 or $x$	+ 3.5 > 2		2	M1 For a correct first step allow $2x = 4 - 7$ or $x + 3.5 = 2$ or an answer of $x = -1.5$ or $x < -1.5$ or $x < -1.5$
				x > -1.5		A1 for $x > -1.5$ oe
	(b)	$(x \pm 8)(x \pm 5)$	$\frac{-(-3) \pm \sqrt{(-3)^2 - 4 \times 1 \times (-40)}}{2 \times 1}$ or $\frac{3 \pm \sqrt{9 + 160}}{2}$			M1 <b>or</b> $(x + a)(x + b)$ where $ab = -40$ <b>or</b> $a + b = -3$ <b>OR</b> correct substitution into quadratic formula (condone one sign error in $a$ , $b$ or $c$ and missing brackets) (if + rather than $\pm$ shown then award M1 only unless recovered with answers)
		(x-8)(x+5)	$\frac{3\pm\sqrt{169}}{2}$ or $\frac{3\pm13}{2}$			M1 $\frac{3\pm\sqrt{169}}{2}$ or $\frac{3\pm13}{2}$
				8, -5	3	A1 dep on at least M1 for correct values
		·				Total 5 marks

<b>8</b> (a)	545 - 500 (= 45) or $592 - 545 (= 47)$		4	M1	may be seen as part of a calcula	ation
	$\frac{45}{500} \times 100 (=9)$ or $\frac{47}{545} \times 100 (=8.6)$			M1	for one correct expression (allocorrect expression for 8.6 throu	
	$\frac{45}{500} \times 100 (=9)$ and $\frac{47}{545} \times 100 (=8.6)$			M1	for both correct expressions <b>or</b> finds 109% of 545: 1.09 × 5456 545 (49.05) or having found "8 500: 1.086 × 500(=543) or 8.69	(=594.05) or 9% of 8.6%" finds 108.6% of
		No, 9(%) and 8.6(%)		A1	for no oe, 9% and 8.6% seen of no oe and 9% and 594.05 or 8.0 No, 49.05 > 45 or No 594.05 >	6% and 543 or
Alternative	e mark scheme for 8(a)					
	$\frac{545}{500} \times 100 (=109) \text{ or } \frac{545}{500} (=1.09) \text{ and}$ $\frac{592}{545} \times 100 (=108.6) \text{ or } \frac{592}{545} (=1.086)$		4	M3	for both correct expressions wh 109 or 1.09 and 108.6 or 1.086 (allow 108 or 108.7 from corre or 1.08 or 1.087 from correct w throughout)  (if not M3 then award M2 for of expressions)	oct working for 108.6 working for 1.086
		No, 109(%) and 108.6(%)		A1	oe eg no and 1.09 and 1.086	
(b)	952 ÷ 85 × 100 oe (=1120)		3	M1	for a method to find price before discount	M2 for $\frac{952}{85} \times 15$
	0.15 × "1120" or "1120" – 952 oe			M1	for a correct method to find discount	
		168		A1		
						Total 7 marks

9	19.3 × 150		2	M1	for $19.3 \times 150$	
		2895		A1	for 2895	
						Total 2 marks

10	$50 \times 60 \ (= 3000) \text{ or } 50 \div 1000 \ (= 0.05 \text{ or } \frac{1}{20})$		3	M1	for 50 with at least one of $\div$ 1000 or $\times$ 60
	or 50 × 60 × 60 (= 180 000) or				or
	$\frac{60 \times 60}{1000} (= 3.6)$				$\frac{60 \times 60}{1000} (=3.6)$
	or $1000 \div 60 \div 60 = 0.27777$ or $\frac{5}{18}$ )				or
	10			3.61	1000 ÷ 60 ÷ 60
	$50 \times \frac{60 \times 60}{1000}$ oe eg $50 \div \frac{5}{18}$			M1	(dep) for a complete method
		180		A1	for 180 (SCB1 for both conversion factors correct but applying them wrongly $eg \frac{50 \times 1000}{60 \times 60})$
					Total 3 marks

11	$(AC^2 =) 17^2 - 15^2$		5	M1	
	$(AC =) \sqrt{17^2 - 15^2} \ (= \sqrt{64} = 8)$			M1	
	$\frac{\pi \times '8'}{2} (= 4\pi = 12.566)$			M1	dep on M2 for $\frac{\pi \times '8'}{2}$ oe or $4\pi$
					12.5663
	'12.566'+ 15 + 17			M1	for '12.566' + 15 + 17 and no additional values
		44.6		A1	for awrt 44.6
					Total 5 marks
Alternative ma	rk scheme for 11				
	$\cos^{-1}\left(\frac{15}{17}\right) (=28.0724) \text{ or } \sin^{-1}\left(\frac{15}{17}\right) (=61.9275)$		5	M1	for a correct method to find one of the angles
	$15 \times \tan (28.0724) (= 8) \text{ or } 15 \div \tan (61.9275) (= 8)$			M1	
	$\frac{\pi \times '8'}{2} \ (= 4\pi = 12.566)$			M1	dep on M2 for $\frac{\pi \times '8'}{2}$ or 12.5663 or $4\pi$
	"12.566" + 15 + 17			M1	for "12.566" + 15 + 17 and no additional values
		44.6		A1	for awrt 44.6
					Total 5 marks

12	Litres per amount of money and then conversion		
	$\frac{8.6 \times 10^5}{770000} (=1.1168)  l/\$$		M1 Number of litres per \$ for D
	$\frac{4.2 \times 10^5}{2500000} (=0.168)  l/k$		M1 Number of litres per Krone for A
	A: <i>l</i> /\$ to <i>l</i> /k '1.1168' ÷ 6.57 (= 0.1699)or D: <i>l</i> /k to <i>l</i> /\$ '0.168' × 6.57 (= 1.103)		M1 <i>l</i> /\$ to <i>l</i> /k for A or <i>l</i> /k to <i>l</i> /\$ for D
		Arctic Oil and relevant figures	A1 for Arctic Oil with 1.1168 and 1.10376 <b>or</b> 0.168 and 0.1699
	Conversion then litres per amount of money		
	$\frac{2500000}{6.57}$ (=380517.5) or 770 000 × 6.57(= 505 8900)		M1 Changing Krone to \$ or \$ to Krone
	$\frac{4.2 \times 10^5}{2500000}$ (=0.168) or $\frac{4.2 \times 10^5}{'380517.5'}$ (=1.103)		M1 Litres per Krone or litres per \$ for D
	$\frac{8.6 \times 10^5}{770000}$ (=1.1168) or $\frac{8.6 \times 10^5}{5058900}$ (=0.1699)		M1 Litres per Krone or litres per \$ for A
		Arctic Oil and relevant figures	A1 for Arctic Oil with 1.1168 and 1.10376 or 0.168 and 0.1699
	Cost per litre then conversion		
	$\frac{2500000}{4.2\times10^5}(=5.952)$		M1 Price per litre in Krone for D
	$\frac{770000}{8.6\times10^5}(0.895)$		M1 Price per litre in \$ for A
	$5.952 \div 6.57 (=0.9059)$ or $0.895 \times 6.57 (=5.882)$		M1 Conversion of Krone to \$ or \$ to Krone

			Arctic Oil and relevant figures	A1	For Arctic Oil with 5.952 and 5.882 <b>or</b> 0.895 and 0.9059
Co	onversion then cost per lit	re			
	500 000 6.57 (=380517.5) or 770	) 000 × 6.57(= 505 8900)		M1	Changing Krone to \$ or \$ to Krone
25 4.2	$\frac{500000}{2\times10^5}$ (= 5.952) or $\frac{'38051}{4.2\times10^5}$	$\frac{17.5'}{10^5}$ (=0.9059)		M1	Cost per litre in Krone or cost per litre in \$ for D
	$\frac{70000}{6\times10^5}$ (= 0.895) or $\frac{'5058}{8.6\times}$			M1	Cost per litre in \$ or cost per litre in Krone for A
			Arctic Oil and relevant figures	A1	For Arctic Oil with 5.952 and 5.882 <b>or</b> 0.895 and 0.9059
Co	omparing equal amounts				
$\frac{8.6}{4.2}$	$\frac{6 \times 10^5}{2 \times 10^5} (= \frac{43}{21} = 2.047)$	$\frac{4.2 \times 10^5}{8.6 \times 10^5} (= \frac{21}{43} = 0.488)$		M1	Multiplier for same amount of D as A or same amount of A as D
	047'×2500 000 K 5119047.619)K	'0.488' × 770 000 \$ (=376046.511)\$		M1	Cost of equal amount of D as A or A as D
= 7	119047.619'÷6.57 779154.88\$ or 0 000×6.57=5058900 K	'376046.511'× 6.57 =2470625.58K or 2500 000÷6.57 = 380517\$		M1	Converts so can compare costs – either K to \$ or original A to K or \$ to K or original D to \$
			Arctic Oil and relevant figures	A1	Arctic Oil and 779154 or with 2470625(figures may be rounded) Or
					Arctic Oil with 5119047 and 5058900 or with 376046 and 380517
Students may	y compare other equal amo	ounts – please use the scheme t	hat best fits their me	thod and a	
					Total 4 marks

13	Angle $CAD = 28^{\circ}$ or angle $ACB = 32^{\circ}$ or angle $ACD = 90^{\circ}$ or angle $ABD = 90^{\circ}$		4	M1	
	ungre Tieb yo or ungre Tibb yo	30°		A1	For a correct answer of 30
	Angles in the same segment are equal, angle in a semicircle is 90° (or angle at centre is double angle at circumference oe) angles in a triangle add up to 180°/angles in a triangle isosceles triangle alternate angles vertically opposite angles (or vertically opposite) angles at a point opposite angles in a cyclic quadrilateral angle between tangent and radius (diameter) alternate segment theorem angles subtended by the same arc(or chord) at the circumference (or on the circle)			B2	Dep on M1 for all correct reasons for their method used (if not B2 then award B1(dep on M1) for a correct circle theorem reason)
					Total 4 marks

14 (a)			2	B1	for $\frac{13}{20}$ and $\frac{7}{20}$ on the first branch (0.65 and 0.35)
		Correct probabilities on the tree diagram		B1	for $\frac{12}{19}$ , $\frac{7}{19}$ , $\frac{13}{19}$ and $\frac{6}{19}$ on the second branch (accept 2 dp or better 0.6315, 0.3684, 0.6842, 0.3157)
(b)	$\frac{7}{20} \times \frac{6}{19}$ oe only		2	M1	ft from (a) as long as probabilities less than 1
	21 190	$\frac{21}{190}$		A1	for $\frac{21}{190}$ oe or 0.11 (at least 2 dp)
					Total 4 marks

15	C, B, E	3	В3	for all 3 correct
			(B2	for 2 correct)
			(B1	for 1 correct)
				Total 3 marks

16	$y^2 = \frac{x+1}{x-4}$		4	M1	for squaring
	x-4 $y^2(x-4) = x+1$ or $y^2x-4y^2 = x+1$			M1	for removing the fraction
	$y^2x - x = 4y^2 + 1$ or $-4y^2 - 1 = x - y^2x$ or $x(y^2 - 1) = 4y^2 + 1$ or $-4y^2 - 1 = x(1 - y^2)$			M1	for expanding the bracket <b>and</b> rearranging for <i>x</i> so that the terms in <i>x</i> are on one side of the correct equation
		$x = \frac{4y^2 + 1}{y^2 - 1}$		A1	for $x = \frac{4y^2 + 1}{y^2 - 1}$ or $x = \frac{-4y^2 - 1}{1 - y^2}$
					(need to see $x =$ somewhere)
					Total 4 marks

17	e.g. $n^2 - (n-1)^2$ or $(n+1)^2 - n^2$		3	M1	for setting up a correct algebraic expression (any letter can be used)
	e.g. $n^2 - n^2 + 2n - 1$ or $n^2 + 2n + 1 - n^2$			M1	Correct expansion of brackets and correct signs or a correct result
		e.g. $2n - 1$ is always odd		A1	dep on M2 for eg $2n - 1$ or $2n + 1$ or $-(2n + 1)$ oe <b>and</b> a suitable conclusion  SCB1 for eg $(2n)^2 - (2n - 1)^2$ or
					$(2n+1)^2 - (2n)^2$ oe
					Total 3 marks

18 (a)	$(0.7 \times 10) + (3.4 \times 5) + (1 \times 9) + (2.5 \times 6) + (4.8 \times 15)$ = 7 + 17 + 9 + 15 + 72 (= 120)  no. of sml squares = $(10 \times 7) + (5 \times 34) + (9 \times 10) + (6 \times 25) + (15 \times 48)$ = 70 + 170 + 90 + 150 + 720 (= 1200)  or all correct values in bars oe not added		3	M1	for a correct method to work out the total area eg total frequency or number of small squares or other correct method (allow one error in method) [count use of 25 for 24 as one error]  or all correct values in bars oe not added
	$(1 \times 7) + (2.5 \times 6) + (5 \times 4.8) = 7 + 15 + 24 (= 46)$ or no. of sml squares $(48 \times 5) + (6 \times 25) + (7 \times 10) = 240 + 150 + 70 (= 460)$			M1	for a correct method to work out the area between 17 minutes and 35 minutes eg using frequency density or number of small squares oe
	$\frac{46}{120}$	$\frac{46}{120}$		A1	for $\frac{46}{120}$ oe (allow 2 dp or better 0.3833 or 38% or better)
(b)			2	M1	for $\frac{n}{15}$ where $n < 15$ or $\frac{q}{720}$ where $q < 720$ or $\frac{r}{72}$ where $r < 72$ or $\frac{9}{m}$ where $m > 9$ or $\frac{432}{p}$ where $p > 432$ $\frac{43.2}{t}$ where $t > 43.2$
		$\frac{9}{15}$		A1	$\frac{9}{15}$ oe
					Total 5 marks

19 (a)		y = -4x + k  (oe)	1	B1	for $y = -4x$ or $y = -4x + k$ where $k$ is any numerical value $k \ne 7$ Could be written in another form e.g. $3y + 12x = 20$
(b)	$m = \frac{-2-1}{23}$ or $m = \frac{12}{-3-2}$ or $-\frac{3}{5}$ or $-0.6$		4	M1	for using $m = \frac{y_2 - y_1}{x_2 - x_1}$
	$m_p = \frac{5}{3}$			M1ft	for using $m_1 \times m_2 = -1$
	$4 = \frac{5}{3}(-6) + c \text{ oe eg } 4 = -10 + c \ (c = 14)$ $y - 4 = \frac{5}{3}(x6)$			M1ft	dep on previous M1 for substituting (-6, 4) into linear equation formula $4 = \frac{5}{3}x + c \text{ to find value of } c \text{ or}$ $y = \frac{5}{3}x + 14 \text{ or } y = 1.66x + 14$
		5x - 3y + 42 = 0		A1	for correct simplified equation where all values are integers $10x - 6y + 84 = 0$ or $3y = 5x + 42$ oe
					Total 5 marks

20	$\frac{18}{\sqrt{7}+1} \times \frac{\sqrt{7}-1}{\sqrt{7}-1}$		3	$     \text{for } \frac{18}{\sqrt{7}+1} \times \frac{\sqrt{7}-1}{\sqrt{7}-1} $
	eg $\frac{18(\sqrt{7}-1)}{7-1}$			M1 Dep on M1 for a correct numerator <b>and</b> multiplying out the denominator to 7 – 1 or 6
	$3\sqrt{7}-3$	$3\sqrt{7}-3$		A1 Dep on M2 Allow $3(\sqrt{7}-1)$
				Total 3 marks

21	(a)(i)		(0, 6)	2	B1	
	(iii)		(2, 6)		B1	
	(b)	eg $(x-4)^2 + 3(x-4) + 4$ oe or eg $(x+\frac{3}{2}-4)^2 - \frac{9}{4} + 4$ oe or eg $x^2 + 3x + 10$ oe or eg $(x+\frac{3}{2})^2 - \frac{9}{4} + 4 + 6$ oe eg $y - 6 = x^2 + 3x + 4$		2	M1	for applying one of the transformations to the equation
			$y = (x-4)^{2} + 3(x-4) + 10$ or $y = (x+\frac{3}{2}-4)^{2} - \frac{9}{4} + 4 + 6$		A1	oe eg $y = (x - \frac{5}{2})^2 + \frac{31}{4}$ or $y = x^2 - 5x + 14$ oe
						Total 4 marks

22	$x^{2} + (x+2)^{2} - 2(x+2) = 24$		5	M1	for substituting linear equation into the
					quadratic equation
	$2x^2 + 2x - 24$ (=0) or $x^2 + x - 12$ (=0)			A1	for a correct equation in the form
	or $2x^2 + 2x = 24$ or $x^2 + x = 12$				$ax^2 + bx + c = 0$ or $ax^2 + bx = -c$
	(x+4)(x-3) (= 0) or			M1ft	dep on M1 for solving their quadratic equation
	$-1\pm\sqrt{1^2-(4\times1\times-12)}$				using any correct method (allow one sign error
	$x = \frac{-1 \pm \sqrt{1^2 - (4 \times 1 \times -12)}}{2 \times 1}$ or				and some simplification – allow as far as
	2				$-1\pm\sqrt{1+48}$
	$\left(x-\frac{1}{2}\right)^2-\left(\frac{1}{2}\right)^2-12=0$				$\frac{-1\pm\sqrt{1+48}}{2}$ ) or if factorising, allow brackets
					which expanded give 2 out of 3 terms correct)
	x = -4 and $x = 3$			A1	for both x values dep on M1
	(-4, -2) and $(3, 5)$	(-4, -2) and $(3, 5)$		A1	for both solutions dep on M1
Alternativ	ve mark scheme for 22			_	
	$(y-2)^2 + y^2 - 2y = 24$		5	M1	for substituting linear equation into the
					quadratic equation
	$2y^2 - 6y - 20$ (=0) or $y^2 - 3y - 10$ (=0)			A1	for a correct equation in the form
	$2y^2 - 6y = 20 \text{ or } y^2 - 3y = 10$				$ay^2 + by + c = 0$ or $ay^2 + by = -c$
	(y-5)(y+2) = 0 or			M1ft	dep on M1 for solving their quadratic equation
	$3 + \sqrt{(3)^2 (4 \times 1 \times 10)}$				using any correct method (allow one sign error
	$y = \frac{3 \pm \sqrt{(-3)^2 - (4 \times 1 \times -10)}}{2 \times 1}$ or				and some simplification – allow as far as
	2/1				$3 \pm \sqrt{9 + 40}$
	$\left(y-\frac{3}{2}\right)^2-\left(\frac{3}{2}\right)^2-10=0$				$\frac{3\pm\sqrt{9+40}}{2}$ ) or if factorising, allow brackets
	$\left(\frac{y-\overline{2}}{2}\right)^{-10-0}$				which expanded give 2 out of 3 terms correct
	y = 5 and $y = -2$			A1	for both y values dep on M1
	y - 3 and $y - 2(-4, -2) and (3, 5)$	(-1, -2) and $(2, 5)$			, 1
	( 4, 2) and (3, 3)	(-4, -2) and $(3, 5)$		A1	for both solutions dep on M1
					Total 5 marks

23	$PM = -\frac{3}{2}\mathbf{a} - \frac{3}{4}\mathbf{b} + 4\mathbf{a} + \frac{1}{2}(2\mathbf{b} - 4\mathbf{a}) \left( = \frac{1}{2}\mathbf{a} + \frac{1}{4}\mathbf{b} \right)$ ULLIM $AM = 4\mathbf{a} + \frac{1}{2}(2\mathbf{b} - 4\mathbf{a}) (= 2\mathbf{a} + \mathbf{b})$ ULLIM $AM = 2\mathbf{b} + \frac{1}{2}(4\mathbf{a} - 2\mathbf{b}) (= 2\mathbf{a} + \mathbf{b})$ ULLIM $MA = \frac{1}{2}(2\mathbf{b} - 4\mathbf{a}) - 2\mathbf{b} (= -2\mathbf{a} - \mathbf{b})$ ULLI $MA = \frac{1}{2}(4\mathbf{a} - 2\mathbf{b}) - 4\mathbf{a} (= -2\mathbf{a} - \mathbf{b})$ ULLI $MA = \frac{1}{2}(4\mathbf{a} - 2\mathbf{b}) - 4\mathbf{a} (= -2\mathbf{a} - \mathbf{b})$		3	M1 for finding PM or AM or MA
	$(AP:PM =) \begin{vmatrix} \frac{3}{2}\mathbf{a} + \frac{3}{4}\mathbf{b} \end{vmatrix} : \begin{vmatrix} \frac{1}{2}\mathbf{a} + \frac{1}{4}\mathbf{b} \end{vmatrix} \text{ oe}$ $(AP:AM =) \begin{vmatrix} \frac{3}{2}\mathbf{a} + \frac{3}{4}\mathbf{b} \end{vmatrix} :  2\mathbf{a} + \mathbf{b}  (= 3:4) \text{ oe}$ $(AM:PM =)  2\mathbf{a} + \mathbf{b}  : \left  \frac{1}{2}\mathbf{a} + \frac{1}{4}\mathbf{b} \right  (= 4:1) \text{ oe}$ $AP = 3PM \text{ oe eg } \frac{3}{2}\mathbf{a} + \frac{3}{4}\mathbf{b} = 3(\frac{1}{2}\mathbf{a} + \frac{1}{4}\mathbf{b}) \text{ oe}$ $AM = \frac{4}{3}AP \text{ oe}$ $AM = 4PM \text{ oe}$			M1 For use of a correct ratio or fraction linking  AP and PM or  AP and AM or  AM and PM  (in either order)  vectors must be in form pa + qb
		3:1		A1
				Total 3 marks

24	$\frac{4(2x-3)-3(2x-5)}{(2x-5)(2x-3)} \text{ or } \frac{8x-12-6x+15}{(2x-5)(2x-3)} \text{ oe}$		4	M1	Writing 1st fraction as a fraction over a common denominator (can be 2 separate fractions)
	x(3-2x)(3+2x) or $(3x-1)(2x-5)$			M1	Complete factorisation of numerator or denominator of 2nd fraction
	$\frac{2x+3}{(2x-5)(2x-3)} \times \frac{(3x-1)(2x-5)}{x(3-2x)(3+2x)}$			M1	may be partially simplified
		$\frac{3x-1}{x(2x-3)(3-2x)}$		A1	e.g. $\frac{3x-1}{x(2x-3)(3-2x)} \text{ or } $ $\frac{1-3x}{x(2x-3)^2} \text{ or } $ $\frac{3x-1}{x(12x-9-4x^2)} \text{ or } $ $\frac{3x-1}{(12x^2-9x-4x^3)} \text{ oe } $ isw for incorrect denominator expansion
					Total 4 marks

25	n = 50		3	B1
	$33125 = \frac{50}{2} [2 \times 50 + (50 - 1) \times k] \text{ oe}$ $33125 = 25 [100 + 49k] \text{ oe}$ $1325 = 100 + 49k \text{ oe}$ $1225 = 49k \text{ oe}$			M1 For correct equation, using formula with $a = 50$ and $n = 50$ substituted (for this mark, allow $n = 49$ )  (k may be written as d)
		25		A1
				Total 3 marks

26	$1600 = \frac{1}{3} \times \pi \times r^2 \times 25 \text{ oe}$		6	M1	for substituting into volume formula for cone correctly and equating to 1600
	eg $r = \sqrt{\frac{1600}{\frac{1}{3}\pi \times 25}}$ or			M1	dep for correct rearrangement of volume formula for $r$
	$r = \sqrt{\frac{192}{\pi}} (= \sqrt{61.1(154)} = 7.8176)$			N/1	Dan an M2 compat mother to find about
	$l = \sqrt{"7.817"^2 + 25^2} (= \sqrt{686.1154} = 26.193)$			M1	Dep on M2 correct method to find slant height of cone (radius of sector)
	$2 \times \pi \times \text{``7.817''} (= 49.1196)$			M1	for using $C = 2\pi r$ oe using figures from correct method
	or				or for using $A = \pi r l$ using figures from
	$\pi \times "7.817" \times "26.193" (= 643.315)$				correct method
	"49.1196" = $2 \times \pi \times$ " 26.193" $\times \frac{x}{360}$			M1	for using arc length = $2\pi r \times \frac{x}{360}$
	or				or
	"643.315" = $\pi \times$ "26.193" $\times \frac{x}{360}$				for using area of sector = $\pi r^2 \times \frac{x}{360}$
		107°	-	A1	for 107° - 108°
					Total 6 marks