

Please check the examination details below before entering your candidate information

Candidate surname

Other names

Centre Number

Candidate Number

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Pearson Edexcel International GCSE

Time 2 hours

Paper
reference

4PM1/02

Further Pure Mathematics PAPER 2



Calculators may be used.

Total Marks

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You must **NOT** write anything on the formulae page.
Anything you write on the formulae page will gain NO credit.

Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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International GCSE in Further Pure Mathematics Formulae sheet

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Mensuration

Surface area of sphere = $4\pi r^2$

Curved surface area of cone = $\pi r \times$ slant height

Volume of sphere = $\frac{4}{3}\pi r^3$

Series

Arithmetic series

Sum to n terms, $S_n = \frac{n}{2}[2a + (n - 1)d]$

Geometric series

Sum to n terms, $S_n = \frac{a(1 - r^n)}{(1 - r)}$

Sum to infinity, $S_\infty = \frac{a}{1 - r} \quad |r| < 1$

Binomial series

$(1 + x)^n = 1 + nx + \frac{n(n - 1)}{2!}x^2 + \dots + \frac{n(n - 1)\dots(n - r + 1)}{r!}x^r + \dots \quad \text{for } |x| < 1, n \in \mathbb{Q}$

Calculus

Quotient rule (differentiation)

$$\frac{d}{dx} \left(\frac{f(x)}{g(x)} \right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

Trigonometry

Cosine rule

In triangle ABC : $a^2 = b^2 + c^2 - 2bc \cos A$

$\tan \theta = \frac{\sin \theta}{\cos \theta}$

$\sin(A + B) = \sin A \cos B + \cos A \sin B$

$\sin(A - B) = \sin A \cos B - \cos A \sin B$

$\cos(A + B) = \cos A \cos B - \sin A \sin B$

$\cos(A - B) = \cos A \cos B + \sin A \sin B$

$\tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$

$\tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$

Logarithms

$\log_a x = \frac{\log_b x}{\log_b a}$



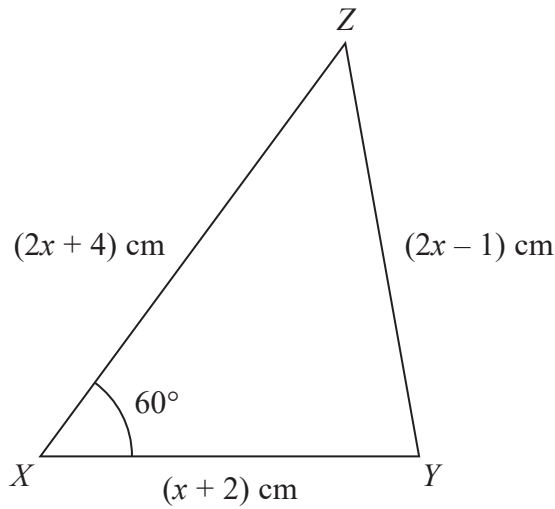


Figure 1

Figure 1 shows triangle XYZ in which

$$XY = (x + 2) \text{ cm} \quad XZ = (2x + 4) \text{ cm} \quad YZ = (2x - 1) \text{ cm} \quad \text{and} \quad \angle YXZ = 60^\circ$$

Find the value of x

Give your answer in the form $p + q\sqrt{3}$ where p and q are integers to be found.

(4)

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Question 2 continued

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(Total for Question 2 is 4 marks)



$$f(x) = 8x^2 + 10x - 3$$

Given that $f(x)$ can be written in the form $A(x + B)^2 + C$ where A , B and C are constants,

(a) find the value of A , the value of B and the value of C . (3)

(b) Hence, or otherwise, find,

(i) the value of x for which $f(x)$ has a minimum,

(ii) the minimum value of $f(x)$. (2)

The curve C has equation $y = f(x)$.

(c) Find the x coordinate of each of the points where C crosses the x -axis. (2)

The straight line l has equation $y = 2x + 13$

(d) Use algebra to find the coordinates of the two points of intersection of C and l . (4)

Using the same axes and the results of parts (b), (c) and (d),

(e) sketch the curve C and the straight line l . (2)

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Question 3 continued

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Question 3 continued

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(Total for Question 3 is 13 marks)



4 The equation of a curve is $y = x^3 \sin x$

Find an equation of the tangent to the curve at the point on the curve where $x = \frac{1}{2}\pi$

Give your answer in the form $y = mx + c$

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Question 4 continued

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(Total for Question 4 is 7 marks)



Question 5 continued

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Question 5 continued

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Question 5 continued

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(Total for Question 5 is 7 marks)



Question 6 continued

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(Total for Question 6 is 8 marks)



Question 7 continued

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Question 7 continued

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Question 7 continued

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(Total for Question 7 is 9 marks)



8 The quadratic equation

$$x^2 - 4k\sqrt{2}x + 2k^4 - 1 = 0$$

where k is a positive constant, has roots α and β

Given that $\alpha^2 + \beta^2 = 66$ and that $\alpha^3 + \beta^3 = p\sqrt{2}$ where p is an integer,

find the value of p

(11)

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Question 8 continued

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Question 8 continued

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(Total for Question 8 is 11 marks)



Question 9 continued

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(Total for Question 9 is 7 marks)



Question 10 continued

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Question 10 continued

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Question 10 continued

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(Total for Question 10 is 13 marks)



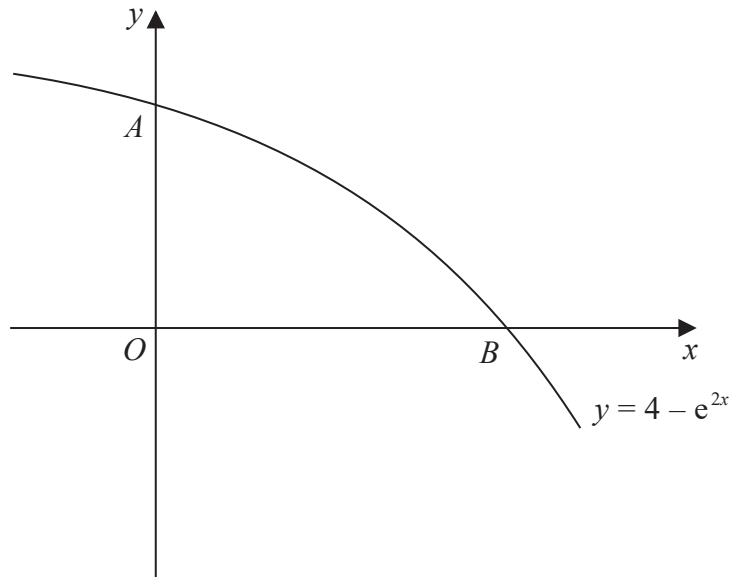


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Figure 3

Figure 3 shows part of the curve C with equation $y = 4 - e^{2x}$. The curve C crosses the y -axis at the point A and the x -axis at the point B .

- (a) (i) Write down the y coordinate of point A .
- (ii) Show that the x coordinate of B is $x = \ln 2$ (3)

The line l is the normal to C at the point B .

- (b) Find an equation for l , giving your answer in the form $y = mx + c$ (4)

The finite region R is bounded by C , l and the y -axis.

- (c) Using calculus, find the area of R .
Give your answer to one decimal place. (7)

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(Total for Question 11 is 14 marks)

TOTAL FOR PAPER IS 100 MARKS

