

Mark Scheme (Results)

Summer 2023

Pearson Edexcel International GCSE In Further Pure Mathematics (4PM1) Paper 02R hrips://britishstudentroom.com/

Edexcel and BTEC Qualifications

hrips://britishstudentroom.com/ Edexcel and BTEC qualifications are awarded by Pearson, the UK's largest awarding body. We provide a wide range of qualifications including academic, vocational, occupational and specific programmes for employers. For further information visit our qualifications websites at <u>www.edexcel.com</u> or <u>www.btec.co.uk</u>. Alternatively, you can get in touch with us using the details on our contact us page at www.edexcel.com/contactus.

Pearson: helping people progress, everywhere

Pearson aspires to be the world's leading learning company. Our aim is to help everyone progress in their lives through education. We believe in every kind of learning, for all kinds of people, wherever they are in the world. We've been involved in education for over 150 years, and by working across 70 countries, in 100 languages, we have built an international reputation for our commitment to high standards and raising achievement through innovation in education. Find out more about how we can help you and your students at: www.pearson.com/uk

Summer 2023 Question Paper Log Number P74284A Publications Code 4PM1_02R_2306_MS All the material in this publication is copyright © Pearson Education Ltd 2023

General Marking Guidance

 All candidates must receive the same treatment. Examiners must mark the last candidate in exactly the same way as they mark the first.

hrips://britishstudentroom.com/

- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification/indicative content will not be exhaustive.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, a senior examiner must be consulted before a mark is given.
- Crossed out work should be marked unless the candidate has replaced it with an alternative response.

Types of mark

- o M marks: method marks
- A marks: accuracy marks
- o B marks: unconditional accuracy marks (independent of M marks)

Abbreviations

- o cao correct answer only
- o ft follow through
- o isw ignore subsequent working
- SC special case
- o oe or equivalent (and appropriate)
- o dep dependent
- o indep independent
- o awrt answer which rounds to
- o eeoo each error or omission

No working

If no working is shown then correct answers normally score full marks If no working is shown then incorrect (even though nearly correct) answers score no marks.

• With working

If the final answer is wrong, always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.

If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.

If a candidate misreads a number from the question. Eg. Uses 252 instead of 255; method marks may be awarded provided the question has not been simplified. Examiners should send any instance of a suspected misread to review.

If there is a choice of methods shown, then award the lowest mark, unless the answer on the answer line makes clear the method that has been used. If there is no answer achieved then check the working for any marks appropriate from the mark scheme.

Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.

Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded to another.

General Principles for Further Pure Mathematics Marking

hrips://britishstudentroom.com/ (but note that specific mark schemes may sometimes override these general principles)

Method mark for solving a 3 term quadratic equation:

1. Factorisation:

$$(x^2+bx+c)=(x+p)(x+q)$$
, where $|pq|=|c|$ leading to $x=...$
 $(ax^2+bx+c)=(mx+p)(nx+q)$ where $|pq|=|c|$ and $|mn|=|a|$ leading to $x=...$

2. Formula:

Attempt to use the **correct** formula (shown explicitly or implied by working) with values for a, b and c, leading to x =

3. Completing the square:

$$x^{2} + bx + c = 0$$
: $(x \pm \frac{b}{2})^{2} \pm q \pm c = 0$, $q \neq 0$ leading to $x = ...$

Method marks for differentiation and integration:

1. Differentiation

Power of at least one term decreased by 1. $(x^n \rightarrow x^{n-1})$

2. Integration:

Power of at least one term increased by 1. $(x^n \rightarrow x^{n+1})$

Use of a formula:

Generally, the method mark is gained by **either**

quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values

or, where the formula is <u>not</u> quoted, the method mark can be gained by implication from the substitution of <u>correct</u> values and then proceeding to a solution.

Answers without working:

The rubric states "Without sufficient working, correct answers may be awarded no marks".

General policy is that if it could be done "in your head" detailed working would not be required. (Mark schemes may override this eg in a case of "prove or show...."

Exact answers:

When a question demands an exact answer, all the working must also be exact. Once a candidate loses exactness by resorting to decimals the exactness cannot be regained.

Rounding answers (where accuracy is specified in the question)

https://britishstudentroom.com/ Penalise only once per question for failing to round as instructed - ie giving more digits in the answers. Answers with fewer digits are automatically incorrect, but the isw rule may allow the mark to be awarded before the final answer is given.

2306 4PM1 Paper 2R Mark Scheme

hers: / britishstidentroom.com/

Question	Scheme	Marks
1	$b^{2} - 4ac = (k+8)^{2} - 4 \times 2 \times k = [k^{2} + 8k + 64]$	M1
	$k^{2} + 8k + 64 = (k+4)^{2} - 16 + 64 = (k+4)^{2} + 48$	dM1A1
	Conclusion: Irrespective of the value of k , $(k+4)^2 \ge 0$ and so	
	$b^2 - 4ac > 0$ therefore the equation will always have distinct	A1
	(real) roots.	[4]
	To	otal 4 marks

Mark	Notes		
M1	Applies the discriminant on the given QE		
	Ignore = 0 , $\geqslant 0$, > 0		
	This must be correct for this mark $\left[\left(k+8\right)^2-4\times2\times k\right]$.		
	Ignore subsequent simplification errors.		
dM1	Completes the square ONLY on their expression for the discriminant		
	provided it is a 3TQ		
	The expression must be of the form $(k+4)^2 \pm X$ where $X \neq 0,64$		
	NB: This mark is dependent on the first M mark.		
	Use of calculus to find $k = -4$ is M0		
A1	For the correct expression.		
A1	For a suitable conclusion.		
	Only accept for this final mark a conclusion as follows [or an		
	equivalent].		
	$(k+4)^2 \ge 0$ and so $(k+4)^2 + 48 > 0$ hence it will always have (real),		
	distinct roots.		
	Note: $(k+4)^2 + 48 \ge 0$ is A0		

		hritos://britishstu
Alterna	ative methods for last 3 marks.	dentroop
ALT 1	finds discriminant of $k^2 + 8k + 64$	n.com
M1	Finds discriminant of their $k^2 + 8k + 64 \Rightarrow D = 64 - 4 \times 1 \times 64 = -192$	
A1	Obtains the correct expression in terms of k with the correct value of D	
A1	Conclusion: $D < 0$ so $k^2 + 8k + 64$ does not have real roots.	
	k^2 is positive so we know it has a minimum so $k^2 + 8k + 64 > 0$	
	This means that $k^2 + 8k + 64 > 0$ and therefore the discriminant	
	will be > 0 meaning that the equation has distinct real roots for all	
	values of k.	

ALT 2	– Uses calculus
M1	$y = k^2 + 8k + 64 \Rightarrow \frac{dy}{dk} = 2k + 8 = 0$ at max/min
A1	So coordinates of max/min are (-4, 48)
	and finds second derivative $\frac{d^2y}{dk^2} = 2$
A1	Conclusion: $\frac{d^2y}{dk^2} = 2 > 0$ hence it is a minimum.
	$(-4, 48)$ is the minimum point and so $k^2 + 8k + 64 > 0$
	This means that $k^2 + 8k + 64 > 0$ and therefore the discriminant will be > 0 meaning that the equation has distinct real roots for all values of k .

ALT 3	– Uses a graph		
M1	Draws a sketch.		
	Graph of $k^2 + 8k + 64$ Accept anywhere in positive y		
A1	The graph is placed correctly with the min point in the 4 th quadrant.		
A1	Conclusion: the graph is always positive with its min point as shown in		
	the diagram. This means that $k^2 + 8k + 64 > 0$ and therefore the		
	discriminant will be > 0 meaning that the equation has distinct real roots		
	for all values of k.		

		hetas://britis	The tude nito on com
Question	Scheme	Marks	Troop
2(a)	$2(x+1) < 5x - 2 \Rightarrow 2x + 2 < 5x - 2 \Rightarrow 3x > 4 \Rightarrow x > \frac{4}{3}$	M1A1 [2]	n.com/
(b)	$3x^2 - x - 10 = 0 \Rightarrow (3x + 5)(x - 2) = 0 \Rightarrow x = -\frac{5}{3}, 2$	M1	
	$\left \frac{5}{3} \right \le x \le 2'$ allow $\left \frac{5}{3} \right < x < 2'$	dM1	
	$\left -\frac{5}{3} \leqslant x \leqslant 2 \right $	A1	
		[3]	
(c)	4,	B1ft	
	$\left \frac{4}{3} < x \le \right 2$	[1]	
	To	tal 6 marks	

Part	Mark	Notes			
(a)	M1	Attempts to solve the inequality with no more than one arithmetical			
		error.			
	A1	For the correct inequality.			
(b)	M1	For attempting to solve the QE to find two critical values.			
	For the d	M and A marks allow any acceptable notation.			
	For exam	For example; $-\frac{5}{3} \leqslant x \cap x \leqslant 2$ or, $-\frac{5}{3} \leqslant x$ and $x \leqslant 2$			
	The region	on must however indicate an INSIDE region			
	dM1	Forms an inside region with their cv's			
		This mark is dependent on the first M mark in (b)			
	A1	For the correct region with the correct inequalities.			
(c)	B1ft	For the correct combined inside region.			
		Penalise the incorrect inequality from part (b) $<$ in place of \le only			
		once.			
		Even if the correct inequality does not follow from their work, award			
		this mark.			

		https://brite	· Strate
Question	Scheme	Marks	"Ditroop
3(a)	$675 = \frac{\theta r^2}{2} \Rightarrow \theta = \frac{675 \times 2}{r^2} = \frac{1350}{r^2}$	M1	'n.com
	$P = 2r + r\theta \Rightarrow P = 2r + r\left(\frac{1350}{r^2}\right) \Rightarrow P = 2r + \frac{1350}{r}$	M1A1 cso	
		[3]	
	$\frac{\mathrm{d}P}{\mathrm{d}r} = 2 - \frac{1350}{r^2}$	M1	
	$2 - \frac{1350}{r^2} = 0 \Rightarrow r = 15\sqrt{3}$ or $\sqrt{675}$	M1A1	
	$P = 2 \times 15\sqrt{3} + \frac{1350}{15\sqrt{3}} = 60\sqrt{3}$	M1A1 [5]	
(c)	$\frac{d^2 P}{dr^2} = \frac{2700}{r^3} r > 0 \Rightarrow \frac{d^2 P}{dr^2} > 0 \Rightarrow minimum$	M1A1ft [2]	
	To	tal 10 marks	

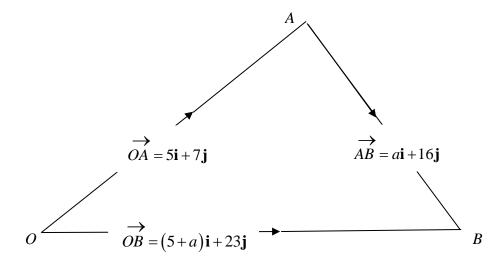
Part Mark **Notes Note:** Accept any variable for *P* in this part of the question for the first two M (a) marks **only**, even no variable as long as it is clear it is the perimeter. Applies the correct formula for the area of a sector with 675 cm² and M1 attempts to rearrange to find an expression for θ , r or $r\theta$ Minimally acceptable expression: $\theta = \frac{k}{r^2}$, $r = \frac{k}{\theta r}$ or $\theta r = \frac{k}{r}$ Applies the **correct** formula for the perimeter of a sector and substitutes M1 their expression for θ provided it is as a minimum of the form $\theta = \frac{k}{r^2}$ Minimally acceptable expression: $P = 2r + \frac{k}{r}$ where k is an integer For a fully correct expression for *P* with no errors seen. **A**1 You must see $P = \dots$ ALT – uses the formula $A = \frac{1}{2}rS$ where S is the arc length. S is very popular! Applies the correct formula for the area of a sector and rearranges to M1find an expression for *S*. $675 = \frac{rS}{2} \Rightarrow S = \frac{1350}{r}$ minimally acceptable $S = \frac{k}{r}$
Applies the correct formula for the perimeter of a sector. M1 $P = 2r + S \Rightarrow P = 2r + \frac{1350}{r}$ minimally acceptable $P = 2r + \frac{k}{r}$ For a fully correct expression for *P* with no errors seen. **A**1 You must see $P = \dots$

		h _{th}	
		Pos. // Br.	
			sh _{stuck}
	ALT 2	– works in degrees	Chiro
	M1	Applies a correct formula for the area of a sector in degrees and attempts to find an expression for θ	St Studentioon Com
		$675 = \frac{\theta}{360} \times \pi r^2 \Rightarrow \theta = \frac{675 \times 360}{\pi r^2} = \frac{243000}{\pi r^2} \qquad \text{Min: } \theta = \frac{K}{\pi r^2}$	
	M1	Applies a correct formula for the perimeter of a sector and substitutes their expression for θ	
		$P = 2r + \frac{\theta}{360} \times 2\pi r \left(\frac{243000}{\pi r^2}\right) \Rightarrow P = 2r + \frac{1350}{r} \text{Min: } P = 2r + \frac{K}{r}$	
		Do not accept solution with a mix of degrees and radians.	
	A1	For a fully correct expression for P with no errors seen. You must see $P = \dots$	
(b)	M1	NB: Allow poor notation here, even $\frac{dy}{dx}$ or nothing at all.	
		For attempting to differentiate the given expression for <i>P</i> The minimally acceptable expression for the derivate is	
		$\frac{dP}{dr} = 2 - \frac{Q}{r^2}$ where Q is a positive integer.	
	M1	For setting their differentiated expression = 0 finding a value for r	
		This is a simple equation to solve. Go through their working checking that it is correct. Do not award this mark for incorrect processing.	
	A1	For $r = 15\sqrt{3}$ oe [An approximate value is $r = 25.98$]	
	NB: A	ward the next 2 marks if they appear in part (b) only]
	M1	For substituting their value for r into the given expression for P	
		Only allow this mark if:	
		• They use the correct <i>r</i> and obtain the correct perimeter.	
		• They use an incorrect r provided it is a positive value and show	
	A1	explicit substitution For the correct final answer in exact form.	
	711	There is no follow through here.	
(c)	NB: Av	ward the next two marks if they appear in part (c) only.	1
	M1	Finds the second derivative.	
		The minimally acceptable expression for the second derivative is	
		$\frac{d^2 P}{dr^2} = \frac{X}{r^3} \text{ where } x \text{ is an integer.} \qquad \text{(The value for } \frac{d^2 P}{dr^2} \text{ is awrt 0.15)}$	
		If they test $\frac{dP}{dr}$ around the minimum point – send to Review.	
	A1ft	If they test <i>P</i> either side – score M0A0 For a correct conclusion.	
		FT their 2nd derivative provided it is of the form $\frac{d^2 P}{dr^2} = \frac{X}{r^3}$	
		r must be positive and if they find a value for $\frac{d^2P}{dr^2}$ then substitution	
		must be seen unless they use $15\sqrt{3}$ and obtain awrt 0.15	

		hitos://brit	SISTURENT CONT. CONT.
Question	Scheme	Marks	Ttroop.
4(a)	$\overrightarrow{OB} = \overrightarrow{OA} + \overrightarrow{AB} = 5\mathbf{i} + 7\mathbf{j} + a\mathbf{i} + 16\mathbf{j} = (5+a)\mathbf{i} + 23\mathbf{j}$	M1A1	n.com/
	$(5\sqrt{29})^2 = (5+a)^2 + 23^2 \Rightarrow 5+a = \pm\sqrt{196} \Rightarrow a = 9, -19$	M1A1	
		[4]	
(b)	$\overrightarrow{AB} = "9"\mathbf{i} + 16\mathbf{j} \Rightarrow \overrightarrow{AB} = \sqrt{"9"^2 + 16^2} = \sqrt{337}$	M1	
	Unit vector: $\frac{1}{\sqrt{"337"}}("9"\mathbf{i}+16\mathbf{j})$ oe.	A1 [2]	
	To	tal 6 marks	

Part	Mark	Notes	
(a)	M1	For the correct vector statement for \overrightarrow{OB} $\overrightarrow{\rightarrow} \rightarrow \rightarrow \rightarrow \rightarrow$ For example, accept $\overrightarrow{AB} = A0 + OB$ This mark can be implied by a correct vector for \overrightarrow{OB}	
	A1	For the correct vector in terms of <i>a</i> [simplified or unsimplified].	
	M1	For using Pythagoras theorem with $(5\sqrt{29})$ and their vector for \overrightarrow{OB} and solving the equation to find two values of a	
	A1	For the two correct values. a = 9, -19 seen in their working	
(b)	M1	For finding $ AB $ by using a correct Pythagoras and writing down the \rightarrow unit vector where $AB = k\mathbf{i} + 16\mathbf{j}$ where k is a positive value. Award for $\frac{"9"\mathbf{i} + 16\mathbf{j}}{\sqrt{"9"^2 + 16^2}}$ $\sqrt{9^2 + 16^2}$ can be implied by sight of $\sqrt{337}$ If they have an incorrect value for a , full substitution using Pythagoras theorem must be seen for the award of this mark.	
	A1	For the correct unit vector. Accept any correct equivalent unit vectors. For example; $\frac{\sqrt{"337"}}{"337"} ("9"\mathbf{i} + 16\mathbf{j}) \text{ or } \frac{"9"\mathbf{i}}{\sqrt{"337"}} + \frac{16\mathbf{j}}{\sqrt{"337"}}$ Accept decimal answers. Eg., $0.054 ("9"\mathbf{i} + 16\mathbf{j})$ for awrt 0.054 Or $0.49\mathbf{i} + 0.87\mathbf{j}$ or better. Allow $\pm \frac{1}{\sqrt{"337"}} ("9"\mathbf{i} + 16\mathbf{j})$	

Useful Sketch



https://britishstudentroom.com/

		hr _{tos://hritings}	
Question	Scheme	Marks	udentroop.
5(a)	$\frac{\mathrm{d}v}{\mathrm{d}t} = 4t - 19$	M1	n.com/
	$\frac{\mathrm{d}v}{\mathrm{d}t} = 4 \times 5 - 19 = 1 \left(\mathrm{m/s^2} \right)$	A1 [2]	
(b)	$2t^2 - 19t + 35 = 0 \Rightarrow (2t - 5)(t - 7) = 0 \Rightarrow t = \frac{5}{2}, 7$	M1	
	$t_1 = \frac{5}{2}$ $t_2 = 7$	A1 [2]	
(c)	$D = \int_{\frac{5}{2}}^{7} (2t^2 - 19t + 35) dt = \left[\frac{2t^3}{3} - \frac{19t^2}{2} + 35t \right]_{\frac{5}{2}}^{7}$	M1	
	$\left[\frac{2 \times 7^3}{3} - \frac{19 \times 7^2}{2} + 35 \times 7 \right] - \left(\frac{2 \times 2.5^3}{3} - \frac{19 \times 2.5^2}{2} + 35 \times 2.5 \right)$	M1	
	$= \left[\frac{49}{6} - \frac{925}{24}\right] = \left[8.167 - 38.542\right] = \left[-\frac{243}{8} \text{ or } -30.375\right]$	A1 [3]	
	$\Rightarrow D = \frac{243}{8}$ (m) oe e.g. 30.375		
		Total 7 marks	

		hr _{ibs://dr.i}	
Part	Mark	Notes	Sh _{Studentroom.com/}
(a)	M1	mark.	M.com/
(b)	M1	For the correct acceleration of 1 m/s². Units are not required. For attempting to solve the given 3TQ for the velocity. A correct method must be used, and they must reach two values of <i>t</i> for the award of this mark. See General Guidance for the definition of an attempt to solve a 3TQ. If there is no visible method seen, both values of <i>t</i> must be seen for the award of this mark.	
	A1	For the two correct values of t They do not need to ne identified as t_1 or t_2 for this mark. Accept $\frac{5}{2}$ and 7 seen.	
(c)	M1	For an attempt to integrate the given expression for <i>v</i> . At least one term must be correct and no terms are to be differentiated. If the value of 35 'disappears' it is M0. The question states 'use calculus' so integration must be seen.	
	M1	For substituting the two values of t into their integrated expression. and subtracting the result (either way) of both substitutions. Allow for any changed expression from v A correct answer of $\pm \frac{243}{8}$ or ± 30.375 implies correct substitution into a correct integral. If the integration is incorrect, or the values are incorrect, full correct substitution must be seen for the award of this mark.	
	A1	For the correct distance (which must be a positive value).	

		https://britis	
Question	Scheme	Marks	RSTIDERTOOM, COM
6(a)		B1	On.com
	$\begin{array}{c} 2 & 2 \\ \alpha^3 + \beta^3 = (\alpha + \beta)^3 - 3\alpha\beta(\alpha + \beta) \end{array}$	M1	
	$\alpha + \beta = -\frac{5}{2} \alpha \beta = -\frac{p}{2}$ $\alpha^{3} + \beta^{3} = (\alpha + \beta)^{3} - 3\alpha\beta(\alpha + \beta)$ $\alpha^{3} + \beta^{3} = \left(-\frac{5}{2}\right)^{3} - 3\left(-\frac{p}{2}\right)\left(-\frac{5}{2}\right) = -\frac{125}{8} - \frac{15p}{4} = -\frac{215}{8}$	M1M1	
	$\Rightarrow p = 3$ ALT	A1 [5]	
	$\alpha^{3} + \beta^{3} = (\alpha + \beta)(\alpha^{2} - \alpha\beta + \beta^{2}) = (\alpha + \beta)((\alpha + \beta)^{2} - 3\alpha\beta)$	[M1]	
(b)	Sum:		
	$\frac{\alpha+\beta}{\alpha^2} + \frac{\alpha+\beta}{\beta^2} = \frac{\alpha\beta^2 + \beta^3 + \alpha^3 + \alpha^2\beta}{\alpha^2\beta^2} = \frac{\alpha^3 + \beta^3 + \alpha\beta(\alpha+\beta)}{\alpha^2\beta^2}$	M1	
	ALT		
	$\frac{\alpha+\beta}{\alpha^2} + \frac{\alpha+\beta}{\beta^2} = \frac{\alpha^2(\alpha+\beta) + \beta^2(\alpha+\beta)}{\alpha^2\beta^2} = \frac{(\alpha^2+\beta^2)(\alpha+\beta)}{\alpha^2\beta^2}$	M1	
	$=\frac{\left(\left(\alpha+\beta\right)^{2}-2\alpha\beta\right)\left(\alpha+\beta\right)}{\alpha^{2}\beta^{2}}$		
	$\frac{\alpha^2 \beta^2}{\frac{-215}{8} + \left(-\frac{3}{2}\right)\left(-\frac{5}{2}\right)} = -\frac{185}{18} \text{allow} \frac{185}{18} \text{if they start with a negative.}$	B1	
	Product:	3.61.4.1	
	$\left(\frac{\alpha+\beta}{\alpha^2}\right) \times \left(\frac{\alpha+\beta}{\beta^2}\right) = \frac{\left(\alpha+\beta\right)^2}{\alpha^2\beta^2} = \frac{\left(-\frac{5}{2}\right)^2}{\left(-\frac{3}{2}\right)^2} = \frac{25}{9}$	M1A1 [5]	
	Equation:		
	$x^{2} + \frac{185}{18}x + \frac{25}{9} = 0 \Rightarrow 18x^{2} + 185x + 50 = 0$ oe		
	Total 1	0 marks	

Part Mark Notes (a) B1 For the correct expression/values for BOTH the sum and product. This must be identified, or implied from their working. M1 For the correct algebra to find $\alpha^3 + \beta^3$ in terms of $\alpha + \beta$ and $\alpha\beta$ • $\alpha^2 + \beta^3 = (\alpha + \beta)^3 - 3\alpha\beta(\alpha + \beta)$ • $\alpha^2 + \beta^3 = (\alpha + \beta)((\alpha + \beta)^2 - 3\alpha\beta)$ • Or any other algebra, but do not award this mark until the values of $\alpha + \beta$ and $\alpha\beta$ can be substituted in directly. M1 For substituting their values of the sum and product into their expression for $\alpha^2 + \beta^3$ M1 For substituting their values of the sum and product into their expression for $\alpha^2 + \beta^3$ A1 For substituting in their working. A1 For the correct value of p with no errors. For the correct algebra for the sum of roots. This must be such that the given value of $\alpha^3 + \beta^3$, with their values of $\alpha\beta$ and $(\alpha + \beta)$ can be substituted in. If they use the ALT they will not need $\alpha^3 + \beta^3$ Some candidates will reverse the sign at this stage in anticipation of the reversal required in the equation. M1 For substituting in the given value for $\alpha^3 + \beta^3$, and their values for $\alpha + \beta$ and $\alpha\beta$ into their expansion for the sum. If they use the ALT they will not need $\alpha^3 + \beta^3$ Bift For the correct value of the product of roots. You must follow through their			hr _{tos.}	
M1 For the correct algebra to find $\alpha^3 + \beta^3$ in terms of $\alpha + \beta$ and $\alpha\beta$ • $\alpha^3 + \beta^3 = (\alpha + \beta)^3 - 3\alpha\beta(\alpha + \beta)$ • $\alpha^3 + \beta^3 = (\alpha + \beta)((\alpha + \beta)^2 - 3\alpha\beta)$ • Or any other algebra, but do not award this mark until the values of $\alpha + \beta$ and $\alpha\beta$ can be substituted in directly. M1 For substituting their values of the sum and product into their expression for $\alpha^3 + \beta^3$ M1 For solving the linear equation in p Allow one slip in their working. A1 For the correct value of p with no errors. (b) M1 For the correct algebra for the sum of roots. This must be such that the given value of $\alpha^3 + \beta^3$, with their values of $\alpha\beta$ and $(\alpha + \beta)$ can be substituted in. If they use the ALT they will not need $\alpha^3 + \beta^3$ Some candidates will reverse the sign at this stage in anticipation of the reversal required in the equation. M1 For substituting in the given value for $\alpha^3 + \beta^3$, and their values for $\alpha + \beta$ and $\alpha\beta$ into their expansion for the sum. If they use the ALT they will not need $\alpha^3 + \beta^3$ B1ft For the correct value of the product of roots. You must follow through their p . You do not need to check the calculation once you see the correct algebra with a correct substitution. M1 For forming an equation with their sum and product. Ft the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. $36x^2 + 370x + 100 = 0$ SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) • If they do not obtain an expansion for the sum into which $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ cannot be directly substituted – first M0 • If they do not substitute $\alpha^3 + \beta^3$, $\alpha\beta$ and α and α and α and α and α and α are a substituted α but of the revalues based on			"I britishs.	
M1 For the correct algebra to find $\alpha^3 + \beta^3$ in terms of $\alpha + \beta$ and $\alpha\beta$ • $\alpha^3 + \beta^3 = (\alpha + \beta)^3 - 3\alpha\beta(\alpha + \beta)$ • $\alpha^3 + \beta^3 = (\alpha + \beta)((\alpha + \beta)^2 - 3\alpha\beta)$ • Or any other algebra, but do not award this mark until the values of $\alpha + \beta$ and $\alpha\beta$ can be substituted in directly. M1 For substituting their values of the sum and product into their expression for $\alpha^3 + \beta^3$ M1 For solving the linear equation in p Allow one slip in their working. A1 For the correct value of p with no errors. (b) M1 For the correct algebra for the sum of roots. This must be such that the given value of $\alpha^3 + \beta^3$, with their values of $\alpha\beta$ and $(\alpha + \beta)$ can be substituted in. If they use the ALT they will not need $\alpha^3 + \beta^3$ Some candidates will reverse the sign at this stage in anticipation of the reversal required in the equation. M1 For substituting in the given value for $\alpha^3 + \beta^3$, and their values for $\alpha + \beta$ and $\alpha\beta$ into their expansion for the sum. If they use the ALT they will not need $\alpha^3 + \beta^3$ B1ft For the correct value of the product of roots. You must follow through their p . You do not need to check the calculation once you see the correct algebra with a correct substitution. M1 For forming an equation with their sum and product. Ft the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equation provided it has integer coefficients. e.g. $36x^2 + 370x + 100 = 0$ SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) • If they do not obtain an expansion for the sum into which $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ cannot be directly substituted – first M0 • If they do not substitute $\alpha^3 + \beta^3$, $\alpha\beta$ and α and α but of the values based on	Part	Mark	Notes	dentro
M1 For the correct algebra to find $\alpha^3 + \beta^3$ in terms of $\alpha + \beta$ and $\alpha\beta$ • $\alpha^3 + \beta^3 = (\alpha + \beta)^3 - 3\alpha\beta(\alpha + \beta)$ • $\alpha^3 + \beta^3 = (\alpha + \beta)((\alpha + \beta)^2 - 3\alpha\beta)$ • Or any other algebra, but do not award this mark until the values of $\alpha + \beta$ and $\alpha\beta$ can be substituted in directly. M1 For substituting their values of the sum and product into their expression for $\alpha^3 + \beta^3$ M1 For solving the linear equation in p Allow one slip in their working. A1 For the correct value of p with no errors. (b) M1 For the correct algebra for the sum of roots. This must be such that the given value of $\alpha^3 + \beta^3$, with their values of $\alpha\beta$ and $(\alpha + \beta)$ can be substituted in. If they use the ALT they will not need $\alpha^3 + \beta^3$ Some candidates will reverse the sign at this stage in anticipation of the reversal required in the equation. M1 For substituting in the given value for $\alpha^3 + \beta^3$, and their values for $\alpha + \beta$ and $\alpha\beta$ into their expansion for the sum. If they use the ALT they will not need $\alpha^3 + \beta^3$ B1ft For the correct value of the product of roots. You must follow through their p . You do not need to check the calculation once you see the correct algebra with a correct substitution. M1 For forming an equation with their sum and product. Ft the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. $36x^2 + 370x + 100 = 0$ SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) • If they do not obtain an expansion for the sum into which $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ cannot be directly substituted – first M0 • If they do not substitute $\alpha^3 + \beta^3$, $\alpha\beta$ and α and α and α and α and α and α are a substituted α but of the revalues based on			For the correct expression/values for BOTH the sum and product.	m.com
 α³ + β³ = (α + β)³ - 3αβ(α + β) α³ + β³ = (α + β)((α + β)² - 3αβ) Or any other algebra, but do not award this mark until the values of α + β and αβ can be substituted in directly. M1 For substituting their values of the sum and product into their expression for α³ + β³ M1 For solving the linear equation in p Allow one slip in their working. A1 For the correct value of p with no errors. (b) M1 For the correct algebra for the sum of roots. This must be such that the given value of α³ + β³, with their values of αβ and (α + β) can be substituted in. If they use the ALT they will not need α³ + β³ Some candidates will reverse the sign at this stage in anticipation of the reversal required in the equation. M1 For substituting in the given value for α³ + β³, and their values for α + β and αβ into their expansion for the sum. If they use the ALT they will not need α³ + β³ B1ft For the correct value of the product of roots. You must follow through their p. You do not need to check the calculation once you see the correct algebra with a correct substitution. M1 For forming an equation with their sum and product. Ft the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. 36x² + 370x + 100 = 0 SC - they solve the equation and find values for α and β Award marks for correct work seen above in part (b) If they do not obtain an expansion for the sum into which α³ + β³, αβ and (α + β) cannot be directly substituted – first M0 If they do not substitute α³ + β³, αβ and (α + β) but other values based on 		M1		
 • α³ + β³ = (α + β)((α + β)² - 3αβ) • Or any other algebra, but do not award this mark until the values of α + β and αβ can be substituted in directly. M1 For substituting their values of the sum and product into their expression for α² + β³ M1 For solving the linear equation in p Allow one slip in their working. A1 For the correct value of p with no errors. (b) M1 For the correct algebra for the sum of roots. This must be such that the given value of α³ + β³, with their values of αβ and (α + β) can be substituted in. If they use the ALT they will not need α³ + β³ Some candidates will reverse the sign at this stage in anticipation of the reversal required in the equation. M1 For substituting in the given value for α³ + β³, and their values for α + β and αβ into their expansion for the sum. If they use the ALT they will not need α³ + β³ B1ft For the correct value of the product of roots. You must follow through their p. You do not need to check the calculation once you see the correct algebra with a correct substitution. M1 For forming an equation with their sum and product. If the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. 36x² + 370x + 100 = 0 SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) If they do not obtain an expansion for the sum into which α³ + β³, αβ and (α + β) cannot be directly substituted – first M0 If they do not substitute α³ + β³, αβ and (α + β) but other values based on 		IVII		
 Or any other algebra, but do not award this mark until the values of α+β and αβ can be substituted in directly. M1 For substituting their values of the sum and product into their expression for α³ + β³ M1 For solving the linear equation in p Allow one slip in their working. A1 For the correct value of p with no errors. (b) M1 For the correct algebra for the sum of roots. This must be such that the given value of α³ + β³, with their values of αβ and (α + β) can be substituted in. If they use the ALT they will not need α³ + β³ Some candidates will reverse the sign at this stage in anticipation of the reversal required in the equation. M1 For substituting in the given value for α³ + β³, and their values for α + β and αβ into their expansion for the sum. If they use the ALT they will not need α³ + β³ B1ft For the correct value of the product of roots. You must follow through their p. You do not need to check the calculation once you see the correct algebra with a correct substitution. M1 For forming an equation with their sum and product. Ft the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. 36x² + 370x + 100 = 0 SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) If they do not obtain an expansion for the sum into which α³ + β³, αβ and (α + β) cannot be directly substituted – first M0 If they do not substitute α² + β³, αβ and (α + β) but other values based on 				
 Walues of α + β and αβ can be substituted in directly. M1 For substituting their values of the sum and product into their expression for α³ + β³ M1 For solving the linear equation in p Allow one slip in their working. A1 For the correct value of p with no errors. (b) M1 For the correct algebra for the sum of roots. This must be such that the given value of α³ + β³, with their values of αβ and (α + β) can be substituted in. If they use the ALT they will not need α³ + β³ Some candidates will reverse the sign at this stage in anticipation of the reversal required in the equation. M1 For substituting in the given value for α³ + β³, and their values for α + β and αβ into their expansion for the sum. If they use the ALT they will not need α³ + β³ B1ft For the correct value of the product of roots. You must follow through their p. You do not need to check the calculation once you see the correct algebra with a correct substitution. M1 For forming an equation with their sum and product. Ft the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0			$\bullet \alpha^3 + \beta^3 = (\alpha + \beta)((\alpha + \beta)^2 - 3\alpha\beta)$	
$\begin{array}{c} \text{expression for} \alpha^3 + \beta^3 \\ \text{M1} \text{For solving the } \textbf{linear} \text{ equation in } p \\ \text{Allow one slip in their working.} \\ \text{A1} \text{For the correct value of } p \text{ with no errors.} \\ \text{(b)} \text{M1} \text{For the correct algebra for the sum of roots.} \\ \text{This must be such that the given value of } \alpha^3 + \beta^3, \text{ with their values of } \alpha\beta \text{ and } (\alpha+\beta) \text{ can be substituted in. If they use the } \textbf{ALT} \text{ they will not need } \alpha^3 + \beta^3 \text{ Some candidates will reverse the sign at this stage in anticipation of the reversal required in the equation.} \\ \text{M1} \text{For substituting in the given value for } \alpha^3 + \beta^3, \text{ and their values for } \alpha+\beta \text{ and } \alpha\beta \text{ into their expansion for the sum.} \\ \text{If they use the } \textbf{ALT} \text{ they will not need } \alpha^3 + \beta^3 \text{ B1ft}} \\ \text{For the correct value of the product of roots.} \\ \text{You must follow through their } p. \\ \text{You do not need to check the calculation once you see the correct algebra with a correct substitution.} \\ \text{M1} \text{For forming an equation with their sum and product.} \\ \text{Ft the sign of their sum. Some candidates reverse the sign when finding the sum.} \\ \text{Watch out for that!} \text{Accept this without = 0} \\ \text{A1} \text{For a correct equation including = 0} \\ \text{There is no follow through on this mark.} \\ \text{NB} \text{ accept a correct equation and find values for } \alpha \text{ and } \beta \\ \text{Award marks for correct work seen above in part (b)} \\ \bullet \text{If they do not obtain an expansion for the sum into which } \alpha^3 + \beta^3, \alpha\beta \text{ and } (\alpha+\beta) \text{ cannot be directly substituted} - \text{first M0} \\ \bullet \text{If they do not substitute } \alpha^3 + \beta^3, \alpha\beta \text{ and } (\alpha+\beta) \text{ but other values based on} \\ \end{array}$				
Allow one slip in their working. A1 For the correct value of p with no errors. For the correct algebra for the sum of roots. This must be such that the given value of $\alpha^3 + \beta^3$, with their values of $\alpha\beta$ and $(\alpha + \beta)$ can be substituted in. If they use the ALT they will not need $\alpha^3 + \beta^3$ Some candidates will reverse the sign at this stage in anticipation of the reversal required in the equation. M1 For substituting in the given value for $\alpha^3 + \beta^3$, and their values for $\alpha + \beta$ and $\alpha\beta$ into their expansion for the sum. If they use the ALT they will not need $\alpha^3 + \beta^3$ B1ft For the correct value of the product of roots. You must follow through their p . You do not need to check the calculation once you see the correct algebra with a correct substitution. M1 For forming an equation with their sum and product. Ft the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. $36x^2 + 370x + 100 = 0$ SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) • If they do not obtain an expansion for the sum into which $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ cannot be directly substituted – first M0 • If they do not substitute $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ but other values based on		M1		
 A1 For the correct value of p with no errors. (b) M1 For the correct algebra for the sum of roots.		M1		
 (b) M1 For the correct algebra for the sum of roots. This must be such that the given value of α³ + β³, with their values of αβ and (α+β) can be substituted in. If they use the ALT they will not need α³ + β³ Some candidates will reverse the sign at this stage in anticipation of the reversal required in the equation. M1 For substituting in the given value for α³ + β³, and their values for α+β and αβ into their expansion for the sum. If they use the ALT they will not need α³ + β³ B1ft For the correct value of the product of roots. You must follow through their p. You do not need to check the calculation once you see the correct algebra with a correct substitution. M1 For forming an equation with their sum and product. Ft the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. 36x² + 370x + 100 = 0 SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) If they do not obtain an expansion for the sum into which α³ + β³, αβ and (α+β) cannot be directly substituted – first M0 If they do not substitute α³ + β³, αβ and (α+β) but other values based on 		A1		
$\alpha\beta \text{ and } (\alpha+\beta) \text{ can be substituted in. If they use the ALT they will not need } \alpha^3+\beta^3$ Some candidates will reverse the sign at this stage in anticipation of the reversal required in the equation. M1 For substituting in the given value for $\alpha^3+\beta^3$, and their values for $\alpha+\beta$ and $\alpha\beta$ into their expansion for the sum. If they use the ALT they will not need $\alpha^3+\beta^3$ B1ft For the correct value of the product of roots. You must follow through their p . You do not need to check the calculation once you see the correct algebra with a correct substitution. M1 For forming an equation with their sum and product. Ft the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. $36x^2+370x+100=0$ SC - they solve the equation and find values for α and β Award marks for correct work seen above in part (b) • If they do not obtain an expansion for the sum into which $\alpha^3+\beta^3$, $\alpha\beta$ and $(\alpha+\beta)$ cannot be directly substituted – first M0 • If they do not substitute $\alpha^3+\beta^3$, $\alpha\beta$ and $(\alpha+\beta)$ but other values based on	(b)	M1	For the correct algebra for the sum of roots.	
not need $\alpha^3 + \beta^3$ Some candidates will reverse the sign at this stage in anticipation of the reversal required in the equation. M1 For substituting in the given value for $\alpha^3 + \beta^3$, and their values for $\alpha + \beta$ and $\alpha\beta$ into their expansion for the sum. If they use the ALT they will not need $\alpha^3 + \beta^3$ B1ft For the correct value of the product of roots. You must follow through their p . You do not need to check the calculation once you see the correct algebra with a correct substitution. M1 For forming an equation with their sum and product. Ft the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. $36x^2 + 370x + 100 = 0$ SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) • If they do not obtain an expansion for the sum into which $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ cannot be directly substituted – first M0 • If they do not substitute $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ but other values based on				
Some candidates will reverse the sign at this stage in anticipation of the reversal required in the equation. M1 For substituting in the given value for α³ + β³, and their values for α + β and αβ into their expansion for the sum. If they use the ALT they will not need α³ + β³ B1ft For the correct value of the product of roots. You must follow through their p. You do not need to check the calculation once you see the correct algebra with a correct substitution. M1 For forming an equation with their sum and product. Ft the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. 36x² + 370x + 100 = 0 SC - they solve the equation and find values for α and β Award marks for correct work seen above in part (b) • If they do not obtain an expansion for the sum into which α³ + β³, αβ and (α + β) cannot be directly substituted – first M0 • If they do not substitute α³ + β³, αβ and (α + β) but other values based on			$\alpha\beta$ and $(\alpha + \beta)$ can be substituted in. If they use the ALT they will	
the reversal required in the equation. M1 For substituting in the given value for $\alpha^3 + \beta^3$, and their values for $\alpha + \beta$ and $\alpha\beta$ into their expansion for the sum. If they use the ALT they will not need $\alpha^3 + \beta^3$ B1ft For the correct value of the product of roots. You must follow through their p . You do not need to check the calculation once you see the correct algebra with a correct substitution. M1 For forming an equation with their sum and product. Ft the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. $36x^2 + 370x + 100 = 0$ SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) • If they do not obtain an expansion for the sum into which $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ cannot be directly substituted – first M0 • If they do not substitute $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ but other values based on				
 M1 For substituting in the given value for α³ + β³, and their values for α + β and αβ into their expansion for the sum. If they use the ALT they will not need α³ + β³ B1ft For the correct value of the product of roots. You must follow through their p. You do not need to check the calculation once you see the correct algebra with a correct substitution. M1 For forming an equation with their sum and product. Ft the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. 36x² + 370x + 100 = 0 SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) If they do not obtain an expansion for the sum into which α³ + β³, αβ and (α + β) cannot be directly substituted – first M0 If they do not substitute α³ + β³, αβ and (α + β) but other values based on 				
$\alpha + \beta \text{ and } \alpha\beta \text{ into their expansion for the sum.}$ If they use the ALT they will not need $\alpha^3 + \beta^3$ B1ft For the correct value of the product of roots. You must follow through their p . You do not need to check the calculation once you see the correct algebra with a correct substitution. M1 For forming an equation with their sum and product. Ft the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. $36x^2 + 370x + 100 = 0$ SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) • If they do not obtain an expansion for the sum into which $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ cannot be directly substituted – first M0 • If they do not substitute $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ but other values based on		M1		
 If they use the ALT they will not need α³ + β³ B1ft For the correct value of the product of roots. You must follow through their p. You do not need to check the calculation once you see the correct algebra with a correct substitution. M1 For forming an equation with their sum and product. Ft the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. 36x² + 370x + 100 = 0 SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) If they do not obtain an expansion for the sum into which α³ + β³, αβ and (α + β) cannot be directly substituted – first M0 If they do not substitute α³ + β³, αβ and (α + β) but other values based on 			,	
 B1ft For the correct value of the product of roots. You must follow through their p. You do not need to check the calculation once you see the correct algebra with a correct substitution. M1 For forming an equation with their sum and product. Ft the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. 36x² + 370x + 100 = 0 SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) If they do not obtain an expansion for the sum into which α³ + β³, αβ and (α + β) cannot be directly substituted – first M0 If they do not substitute α³ + β³, αβ and (α + β) but other values based on 				
 You do not need to check the calculation once you see the correct algebra with a correct substitution. M1 For forming an equation with their sum and product. Ft the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. 36x² + 370x + 100 = 0 SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) If they do not obtain an expansion for the sum into which α³ + β³, αβ and (α + β) cannot be directly substituted – first M0 If they do not substitute α³ + β³, αβ and (α + β) but other values based on 		B1ft		
algebra with a correct substitution. M1 For forming an equation with their sum and product. Ft the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. 36x² + 370x + 100 = 0 SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) • If they do not obtain an expansion for the sum into which α³ + β³, αβ and (α + β) cannot be directly substituted – first M0 • If they do not substitute α³ + β³, αβ and (α + β) but other values based on				
M1 For forming an equation with their sum and product. Ft the sign of their sum. Some candidates reverse the sign when finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. $36x^2 + 370x + 100 = 0$ SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) • If they do not obtain an expansion for the sum into which $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ cannot be directly substituted – first M0 • If they do not substitute $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ but other values based on				
finding the sum. Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. $36x^2 + 370x + 100 = 0$ SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) • If they do not obtain an expansion for the sum into which $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ cannot be directly substituted – first M0 • If they do not substitute $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ but other values based on		M1		
Watch out for that! Accept this without = 0 A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. $36x^2 + 370x + 100 = 0$ SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) • If they do not obtain an expansion for the sum into which $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ cannot be directly substituted – first M0 • If they do not substitute $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ but other values based on			1	
A1 For a correct equation including = 0 There is no follow through on this mark. NB accept a correct equivalent equation provided it has integer coefficients. e.g. $36x^2 + 370x + 100 = 0$ SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) • If they do not obtain an expansion for the sum into which $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ cannot be directly substituted – first M0 • If they do not substitute $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ but other values based on				
NB accept a correct equivalent equation provided it has integer coefficients. e.g. $36x^2 + 370x + 100 = 0$ SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) • If they do not obtain an expansion for the sum into which $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ cannot be directly substituted – first M0 • If they do not substitute $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ but other values based on		A1		
coefficients. e.g. $36x^2 + 370x + 100 = 0$ SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) • If they do not obtain an expansion for the sum into which $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ cannot be directly substituted – first M0 • If they do not substitute $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ but other values based on				
SC – they solve the equation and find values for α and β Award marks for correct work seen above in part (b) • If they do not obtain an expansion for the sum into which $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ cannot be directly substituted – first M0 • If they do not substitute $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ but other values based on				
 Award marks for correct work seen above in part (b) If they do not obtain an expansion for the sum into which α³ + β³, αβ and (α + β) cannot be directly substituted – first M0 If they do not substitute α³ + β³, αβ and (α + β) but other values based on 		SC – the		
 If they do not obtain an expansion for the sum into which α³ + β³, αβ and (α + β) cannot be directly substituted – first M0 If they do not substitute α³ + β³, αβ and (α + β) but other values based on 			-	
$(\alpha + \beta)$ cannot be directly substituted – first M0 • If they do not substitute $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ but other values based on				
• If they do not substitute $\alpha^3 + \beta^3$, $\alpha\beta$ and $(\alpha + \beta)$ but other values based on				
		`		
α and β - second into			$d\beta$ - second M0	
• If they cannot substitute $\alpha\beta$ and $(\alpha + \beta)$ into the product – B0				
Then allow marks for forming the equation as above.				

$ \begin{array}{ c c c }\hline \textbf{Question} & \textbf{Scheme} & \textbf{Marks} \\ \hline \textbf{7(a)} & \left(\cos 3\theta + \sqrt{3}\sin 3\theta\right)^{\frac{1}{2}} = 0 \Rightarrow \cos 3\theta = -\sqrt{3}\sin 3\theta \Rightarrow \tan 3\theta = -\frac{1}{\sqrt{3}} & \text{M1} \\ & \Rightarrow 3\theta = -\frac{\pi}{6} & \text{or } \frac{5\pi}{6} & \text{A1} \\ & \Rightarrow m = -\frac{\pi}{18} & n = \frac{5\pi}{18} & \text{[3]} \\ \hline \textbf{(b)} & V = \pi \int_{\frac{18}{18}}^{\frac{5\pi}{18}} \left(\cos 3\theta + \sqrt{3}\sin 3\theta\right) d\theta & \text{M1} \\ & V = \pi \left[\frac{\sin 3\theta}{3} - \frac{\sqrt{3}\cos 3\theta}{3}\right]_{\frac{\pi}{18}}^{\frac{5\pi}{18}} & \text{M1} \\ & V = \pi \left[\frac{\sin 3\left(\frac{5\pi}{18}\right)}{3} - \frac{\sqrt{3}\cos 3\left(\frac{5\pi}{18}\right)}{3}\right] - \left(\frac{\sin 3\left(-\frac{\pi}{18}\right)}{3} - \frac{\sqrt{3}\cos 3\left(-\frac{\pi}{18}\right)}{3}\right)\right] & \text{M1} \\ & V = \frac{4\pi}{2} & \text{A1} \\ & V = \frac{4\pi}{2} & \text{A1} \\ & V = \frac{4\pi}{2} & \text{A1} \\ & V = \frac{4\pi}{2} & \text{A2} \\ & V = \frac{4\pi}{2} & \text{A3} \\ & V = \frac{\pi}{2} & \text{A3} \\ & V = \frac{\pi}{2} & \text{A4} \\ & V = \frac$		h _{rho}	https://britishst.	
$\Rightarrow m = -\frac{\pi}{18} n = \frac{5\pi}{18}$ $V = \pi \int_{-\frac{\pi}{18}}^{\frac{5\pi}{18}} (\cos 3\theta + \sqrt{3} \sin 3\theta) d\theta$ $V = \pi \left[\frac{\sin 3\theta}{3} - \frac{\sqrt{3} \cos 3\theta}{3} \right]_{-\frac{\pi}{18}}^{\frac{5\pi}{18}}$ $V = \pi \left[\frac{\sin 3\left(\frac{5\pi}{18}\right)}{3} - \frac{\sqrt{3} \cos 3\left(\frac{5\pi}{18}\right)}{3} \right] - \left(\frac{\sin 3\left(-\frac{\pi}{18}\right)}{3} - \frac{\sqrt{3} \cos 3\left(-\frac{\pi}{18}\right)}{3} \right) \right]$ $V = \frac{4\pi}{2}$ $M1$ $V = \frac{4\pi}{2}$ $M1$	Question		4dep	25
$\Rightarrow m = -\frac{\pi}{18} n = \frac{5\pi}{18}$ $V = \pi \int_{-\frac{\pi}{18}}^{\frac{5\pi}{18}} (\cos 3\theta + \sqrt{3} \sin 3\theta) d\theta$ $V = \pi \left[\frac{\sin 3\theta}{3} - \frac{\sqrt{3} \cos 3\theta}{3} \right]_{-\frac{\pi}{18}}^{\frac{5\pi}{18}}$ $V = \pi \left[\left(\frac{\sin 3\left(\frac{5\pi}{18}\right)}{3} - \frac{\sqrt{3} \cos 3\left(\frac{5\pi}{18}\right)}{3} \right) - \left(\frac{\sin 3\left(-\frac{\pi}{18}\right)}{3} - \frac{\sqrt{3} \cos 3\left(-\frac{\pi}{18}\right)}{3} \right) \right]$ $V = \frac{4\pi}{2}$ $M1$ $V = \frac{4\pi}{2}$ $M1$	7(a)	$\left(\cos 3\theta + \sqrt{3}\sin 3\theta\right)^{\frac{1}{2}} = 0 \Rightarrow \cos 3\theta = -\sqrt{3}\sin 3\theta \Rightarrow \tan 3\theta = -\frac{1}{\sqrt{3}}$	M1	n.com
$\Rightarrow m = -\frac{\pi}{18} n = \frac{5\pi}{18}$ $V = \pi \int_{-\frac{\pi}{18}}^{\frac{5\pi}{18}} (\cos 3\theta + \sqrt{3} \sin 3\theta) d\theta$ $V = \pi \left[\frac{\sin 3\theta}{3} - \frac{\sqrt{3} \cos 3\theta}{3} \right]_{-\frac{\pi}{18}}^{\frac{5\pi}{18}}$ $V = \pi \left[\left(\frac{\sin 3\left(\frac{5\pi}{18}\right)}{3} - \frac{\sqrt{3} \cos 3\left(\frac{5\pi}{18}\right)}{3} \right) - \left(\frac{\sin 3\left(-\frac{\pi}{18}\right)}{3} - \frac{\sqrt{3} \cos 3\left(-\frac{\pi}{18}\right)}{3} \right) \right]$ $V = \frac{4\pi}{2}$ $M1$ $V = \frac{4\pi}{2}$ $M1$		$\Rightarrow 3\theta = -\frac{\pi}{6} \text{ or } \frac{5\pi}{6}$	A1	
(b) $V = \pi \int_{\frac{\pi}{18}}^{\frac{5\pi}{18}} (\cos 3\theta + \sqrt{3} \sin 3\theta) d\theta$ $V = \pi \left[\frac{\sin 3\theta}{3} - \frac{\sqrt{3} \cos 3\theta}{3} \right]_{\frac{\pi}{18}}^{\frac{5\pi}{18}}$ $V = \pi \left[\left(\frac{\sin 3\left(\frac{5\pi}{18}\right)}{3} - \frac{\sqrt{3} \cos 3\left(\frac{5\pi}{18}\right)}{3} \right) - \left(\frac{\sin 3\left(-\frac{\pi}{18}\right)}{3} - \frac{\sqrt{3} \cos 3\left(-\frac{\pi}{18}\right)}{3} \right) \right]$ $V = \frac{4\pi}{2}$ $A1$		$\Rightarrow m = -\frac{\pi}{18}$ $n = \frac{5\pi}{18}$		
$V = \pi \left[\left(\frac{\sin 3 \left(\frac{5\pi}{18} \right)}{3} - \frac{\sqrt{3}\cos 3 \left(\frac{5\pi}{18} \right)}{3} \right) - \left(\frac{\sin 3 \left(-\frac{\pi}{18} \right)}{3} - \frac{\sqrt{3}\cos 3 \left(-\frac{\pi}{18} \right)}{3} \right) \right] $ $V = \frac{4\pi}{3}$ $A1$	(b)	$V = \pi \int_{-\frac{\pi}{18}}^{\frac{5\pi}{18}} \left(\cos 3\theta + \sqrt{3}\sin 3\theta\right) d\theta$	M1	
$V = \frac{4\pi}{3}$		18		
$V = \frac{4\pi}{3}$		$V = \pi \left[\left(\frac{\sin 3\left(\frac{5\pi}{18}\right)}{3} - \frac{\sqrt{3}\cos 3\left(\frac{5\pi}{18}\right)}{3} \right) - \left(\frac{\sin 3\left(-\frac{\pi}{18}\right)}{3} - \frac{\sqrt{3}\cos 3\left(-\frac{\pi}{18}\right)}{3} \right) \right]$	M1	
		$V = \frac{4\pi}{3}$	A1 [4]	

Part	Mark	Notes		
(a)	M1	Sets the equation = 0 and obtains $\tan 3\theta = k$		
	A1	Finds at least one correct value of 3θ		
		$3\theta = -\frac{\pi}{6} \text{or} \frac{5\pi}{6}$		
		Works in degrees		
		Accept -30° or 150° for this mark.		
		This mark is also implied by one correct solution for m or n in degrees or		
		radians.		
		NB This is an M mark in Epen		
	A1	For $m = -\frac{\pi}{18}$ $n = \frac{5\pi}{18}$ which must be in radians.		
		Accept embedded in coordinates.		
		M and n do not need to be identified.		

(b)	Working in degrees.
	Allow working in deg

Allow working in degrees up to the last M mark.					
M1	For a correct statement for the volume of revolution with π and their limits.				
	Allow				

$$V = \pi \int_{\frac{-\pi}{18}}^{\frac{5\pi}{18}} \left[\left[\cos 3\theta + \sqrt{3} \sin 3\theta \right]^{\frac{1}{2}} \right]^{2} d\theta \text{ or } V = \pi \int_{\frac{-\pi}{18}}^{\frac{5\pi}{18}} \left(\cos 3\theta + \sqrt{3} \sin 3\theta \right) d\theta$$

Allow also:

$$V = \pi \int_{\frac{\pi}{18}}^{\frac{5\pi}{18}} \left(\cos 3\theta + \sqrt{3}\sin 3\theta\right) dx \text{ or even } V = \pi \int_{\frac{\pi}{18}}^{\frac{5\pi}{18}} \left(\cos 3\theta + \sqrt{3}\sin 3\theta\right)$$

This mark can be implied by correct further working

Working in degrees

$$V = \pi \int_{-10^{\circ}}^{50^{\circ}} \left(\cos 3\theta + \sqrt{3}\sin 3\theta\right) d\theta$$

M1 For an acceptable attempt at integration.

Minimally acceptable integration is as follows.

$$\cos 3\theta \Rightarrow \pm \frac{\sin 3\theta}{3}, \quad \sin 3\theta \Rightarrow \pm \frac{\cos 3\theta}{3}$$

Ignore absence or incorrect limits and the absence of π for this mark.

M1 For substitution of the correct limits into their integrated expression the correct way around. This must be a changed expression from the one given.

If the integrated expression is correct with correct limits, allow a final volume of $\frac{4\pi}{3}$ seen without explicit substitution. If the final volume is incorrect without evidence of explicit substitution award M0.

If the integrated expression is incorrect or the limits are incorrect, explicit substitution **must** be seen for the award of this mark.

Do not allow use of degrees at this stage.

Ignore absence of π for this mark.

A1 For the correct volume $(V) = \frac{4\pi}{3}$

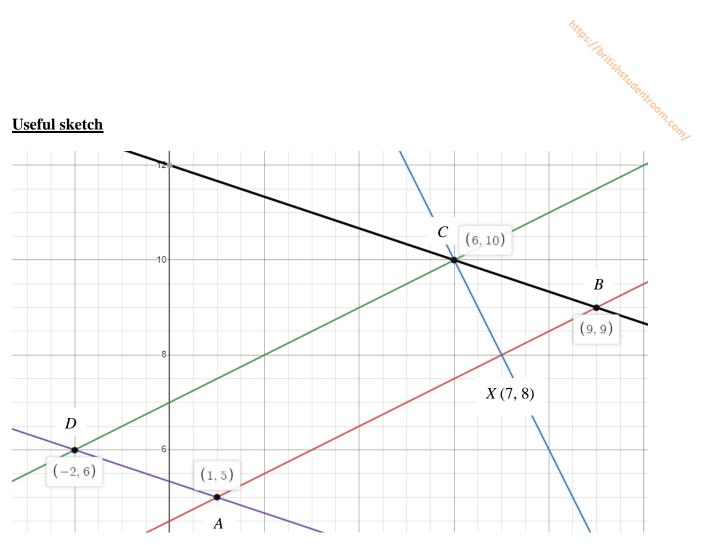
		hrips://brite	The tide rito on conf
Question	Scheme	Marks	Studentroo.
8(a)	$\frac{y-5}{5-9} = \frac{x-1}{1-9}$ $\Rightarrow x-2y+9=0$	M1A1 A1 [3]	M.com/
(b)	$ \frac{\text{Coordinates of point } X}{\left(\frac{3\times9+1\times1}{3+1}, \frac{3\times9+1\times5}{3+1}\right)} = (7,8) $	B1B1	
	The perpendicular gradient = $-\frac{1}{\frac{1}{2}} = -2$	B1ft	
	Equation of l $y-8=-2(x-7) \Rightarrow y=-2x+22 *$	M1A1	
		cso [5]	
(c)	$y = -2(6) + 22 \Rightarrow p = 10$	B1 [1]	
(d)	$\overrightarrow{BA} = \begin{pmatrix} 1-9 \\ 5-9 \end{pmatrix} = \begin{pmatrix} -8 \\ -4 \end{pmatrix} \Rightarrow \overrightarrow{CD} = \begin{pmatrix} 6-8 \\ 10-4 \end{pmatrix} = \begin{pmatrix} -2 \\ 6 \end{pmatrix}$	M1	
	and coordinates of C are $(6, 10)$ so coordinates of D are $(-2, 6)$	A1A1 [3]	
(e)	Length of AB (or CD) = $\sqrt{(9-5)^2 + (9-1)^2} = \sqrt{80}$	B1	
	Length of $CX = \sqrt{(10-8)^2 + (7-6)^2} = \sqrt{5}$	B1	
	Area of parallelogram $ABCD = \sqrt{5} \times \sqrt{80} = \sqrt{400} = 20 \text{ (units}^2\text{)}$	M1A1 [4]	
	Total	16 marks	

Part	Mark	Notes		
(a)	M1	For using a correct method and the given coordinates of A and B to form		
		the equation of AB. Do not score this mark until they find the gradient		
		and form the equation of the line using a correct formula.		
		If they use $y = mx + c$ do not allow this mark until they find c and form		
		a complete equation.		
		$\left[m = \frac{1}{2}, c = \frac{9}{2} y = \frac{x}{2} + \frac{9}{2} \right]$		
	A 1	For the correct equation of AB in any form.		
	A 1	For the correct equation of AB in the required form.		

		h _{rbs}	
		"H _{Britishs}	
		*Fidention	
(b)	B1	For either x or y correct coordinates of point X NB This is an M mark in Epen	n.com
	B1	For both x and y correct coordinates of point X NB This is an A mark in Epen.	
	B1ft	For writing down the inverse reciprocal of their gradient for <i>AB</i> Ft their gradient form part (a)	
	M1	For forming an equation for l using their coordinates of X and their negative reciprocal gradient of AB $y-8=-2(x-7) \Rightarrow y=-2x+22$	
	A1	For the correct equation of <i>l</i> as shown.	
(c)	B1	For $y = 10$	
(d)	M1	For a suitable method. Method 1 - Uses vectors: $\overrightarrow{BA} = \begin{pmatrix} 1-9 \\ 5-9 \end{pmatrix} = \begin{pmatrix} -8 \\ -4 \end{pmatrix} \Rightarrow \overrightarrow{CD} = \begin{pmatrix} 6+(-8) \\ 10+(-4) \end{pmatrix} \Rightarrow \begin{bmatrix} -2 \\ 6 \end{bmatrix}$ OR: $\overrightarrow{BC} = \begin{pmatrix} 6-9 \\ 9-10 \end{pmatrix} = \begin{pmatrix} -3 \\ -1 \end{pmatrix} \Rightarrow \overrightarrow{AD} = \begin{pmatrix} 1-3 \\ 5-(-1) \end{pmatrix} \Rightarrow \begin{bmatrix} -2 \\ 6 \end{pmatrix}$	
		Method 2 - Uses simultaneous equations: The equation of AD is $y = -\frac{x}{3} + \frac{16}{3}$ and of CD is $y = \frac{x}{2} + 7$	
		$-\frac{x}{3} + \frac{16}{3} = \frac{x}{2} + 7 \Rightarrow x = -2 \text{ and } y = 6$	
		Method 3 - Uses the gradient and length of AB or CD	
		$AB = CD = 4\sqrt{5} = \sqrt{(6-x)^2 + (y-10)^2}$	
		Gradient: $\frac{1}{2} = \frac{10 - y}{6 - x} \Rightarrow x = 2y - 14$	
		$\left(4\sqrt{5}\right)^2 = \left(6 - \left(2y - 14\right)\right)x^2 + \left(y - 10\right)^2 \Rightarrow 5y^2 - 100y + 420 = 0$	
		$\Rightarrow y = 6, 14 \text{ and } x = -2, 14$	
		Allow no more than one error in either method.	
	A1	For either correct x or y coordinate of D $[(-2, 6)]$	
	A1	NB this is an A mark in Epen For both correct coordinates of D	
	***	(-2,6)	

		Artios:// Britis	Shstudentroom.com/
(e)	B1	For the correct length of either <i>AB</i> [<i>CD</i>] or <i>CX</i>	TOO,
		These are given coordinates there is no ft	n.con
	B1	For the correct lengths of both AB [CD] and CX Ft their C and their X	2
	M1	For using a correct method to calculate the area of a parallelogram.	
		$b \times h = CX \times AB = \sqrt{5} \times \sqrt{80} = \sqrt{400} = 20$	
		If their lengths are incorrect allow this mark provided their lengths are identified as base and perpendicular height.	
		If they use AD as the base $\left[\sqrt{10}\right]$, the perpendicular height required is	
		$2\sqrt{10}$ so base \times height = $\sqrt{10} \times 2\sqrt{10} = \dots$	
	A1	For the correct area of 20 [units ²]	
	ALT – 1	Using determinants	
	B1B1	For sight of the correct array which must use the coordinates of A , B , C and D ONLY. The coordinates $(7, 8)$ seen in the array is B0B0 $ \begin{pmatrix} 1 & 9 & '6' & '-2' & 1 \\ 5 & 9 & '10' & '6' & 5 \end{pmatrix} $	
		Award both marks for fully correct. Award B1 if there are no more than	
		2 errors but with none missing. There must be 5 sets of coordinates in	
		the array with first and last the same. The coordinates must go in	
	3.54	order around the parallelogram clockwise or anticlockwise.	
	M1	For the correct evaluation of their 2×5 array. Allow this even if they	
		have (7, 8) included instead of (9, 9) [which is a common error]	
		$ \frac{1}{2} \begin{pmatrix} 1 & 9 & 6 & -2 & 1 \\ 5 & 9 & 10 & 6 & 5 \end{pmatrix} = \frac{1}{2} \left[\left[(9 + 90 + 36 - 10) - (45 + 54 - 20 + 6) \right] \right] = \dots $	
	A1	For the correct area of 20 [units ²]	

Useful sketch



		https://hrite	The finder froom com
Question	Scheme	Marks	iroom,
9(a)	(i) $y = -2$ (ii) $x = -6$	B1 B1 [2]	COM
(b)	(i) $\left(\frac{3}{2},0\right)$	B1	
	(ii) $\left(0,\frac{1}{2}\right)$	B1 [2]	
(c)	20	B1 – shape	
		B1ft-	
		Asymptotes	
	(0, 0.5)	B1ft –	
		Intersections [3]	
	$-\frac{-20}{-20} - \frac{-10}{-20} - \frac{-10}{-20} - \frac{-10}{-20} - \frac{-10}{-20} - \frac{-20}{-20} -$		
	(1.5, 0) $x = -6$		
(d)	$\frac{dy}{dx} = \frac{(x+6)(-2)-(3-2x)(1)}{(x+6)^2}$	M1A1	
	$\frac{dy}{dx} = \frac{-15}{(x+6)^2}$ with conclusion; numerator negative,	A1 [3]	
	denominator always positive, $\stackrel{-}{\underset{+}{\longrightarrow}}$ negative		
(e)	$\frac{-15}{(x+6)^2} = -\frac{3}{5} \Rightarrow 25 = (x+6)^2 \Rightarrow x = -6 \pm 5 = -11, -1$	M1A1	
	$y = \frac{3 - 2(-1)}{-1 + 6} = 1$	B1	
	$y-1=-\frac{3}{5}(x-[-1]) \Rightarrow y=-\frac{3}{5}x+\frac{2}{5} \Rightarrow k=\frac{2}{5}$	M1A1 [5]	
	Te	otal 15 marks	

		h _{thos://b.}	
Dowt	Moule	Notes	Shstudentoon, con/
Part (a)	Mark B1	Notes For the correct equation.	On.co
(i)	Б1	given only. For example, the following presentation is B0B0 $x = -6$	37
(ii)	D1	y = -2	_
(b)	B1 If their	For the correct equation. coordinates are not labelled (i) and (ii) or are given in the incorrect place	_
	[for exa	ample, (b)(i) $y = \frac{1}{2}$ is B0] accept them in the order given only. For	
	exampl	e, the following presentation is B0B0	
	$\left(0,\frac{1}{2}\right)$		
	$\left(\frac{3}{2},0\right)$		
(i)	B1	For the correct coordinates. Accept $x = \frac{3}{2}$	
(ii)	B1	For the correct coordinates. Accept $y = \frac{1}{2}$	
(c)	B1	For the correct shape with two branches the correct way around anywhere in the grid. It must be asymptotic in nature. The ends of the curve must not come back on themselves. Whilst you need to be fairly generous, any obvious turning back is B0	
	B1ft	For the correct asymptotes drawn and labelled with at least one branch of the curve [which must be asymptotic in nature in at least one branch] in the correct place seen. Ft their asymptotes Accept the vertical line drawn shown passing through their -6 and the horizontal line drawn shown passing through their -2	
	B1ft	For the correct coordinates of intersections with the relevant branch of the curve drawn correctly seen. The curve must go through the points. Do not accept touching the axis. Allow $\frac{1}{2}$ marked on y-axis and $\frac{3}{2}$ marked on the x-axis. Ft their coordinates of intersections.	
(d)	M1	 For an attempt at quotient rule. The denominator must be squared, or accept (x+6)(x+6) or x²+12x+36 Both (x+6) and (3-2x) differentiated correctly. 	
	A1 A1	 The two terms in the numerator subtracted either way around. Fully correct derivative (simplification not required for this mark). For a correct simplified derivative with a correct conclusion. 	
	111	For example: $(x+6)^2 \ge 0$, -15 is negative, $\frac{\text{negative}}{\text{positive}}$ is always	
		negative. [Accept also $(x+6)^2 > 0$]	

		Treps.	Tidentoon.com/
		Torrish	v.
			Cudentro.
			OM. COM
(e)	M1	For setting the value of $-\frac{3}{5}$ = their $\frac{dy}{dx}$ with an attempt to find at least	
		one value of x . Allow this even if their derivative results in a linear	
	A1	equation. For both correct values of <i>x</i>	
	B1	For $y = 1$ using $x = -1$	
		OR	
		For $y = -5$ using $x = -11$	
	M1	For forming an equation of the line with either	
		x = -1, $y = 1$ or $x = -11$, $y = -5$ or their x and their y	
	A1	For the correct value of <i>k</i> (accept an embedded value).	
		$y = -\frac{3}{5}x + \frac{2}{5} \Rightarrow k = \frac{2}{5}$	
		5 5 5	
		You can award this mark even if the previous A mark has not been	
		scored. So, for a correct solution without showing that $x = -11$ score	
		M1A0B1M1A1	
	ALT fo	or last 3 marks	
	B1	Sets $-\frac{3}{5}x + k = \frac{3 - 2x}{x + 6}$	
	M1	Substitutes $x = -1$ or -11 into the above equation	
	A1	For $k = \frac{2}{5}$	
		You can award this mark even if the previous A mark has not been	
		scored. So, for a correct solution without showing that $x = -11$ score M1A0B1M1A1	
		WITAUDIWITAI	

		hrtos://britishstud	۶ ₂ ,
Question	Scheme	Marks	Croop
10	8log ₄ 64	M1	7.00
	$8\log_{x} 64 = \frac{8\log_{4} 64}{\log_{4} x}$ $\log_{4} x^{3} = 3\log_{4} x$	M1	V
	$\log_4 x^3 + 8\log_x 64 = 22 \Rightarrow 3\log_4 x + \frac{8\log_4 64}{\log_4 x} = 22$ $\Rightarrow 3(\log_4 x)^2 + 8\log_4 64 = 22\log_4 x \Rightarrow 3(\log_4 x)^2 - 22\log_4 x + 24 = 0$	M1	
	$3(\log_4 x)^2 - 22\log_4 x + 24 = 0 \Rightarrow (3\log_4 x - 4)(\log_4 x - 6) = 0$	M1	
	$\Rightarrow \log_4 x = \frac{4}{3}, 6$	A1	
	$x = 4^{\frac{4}{3}}$ or awrt 6.35 and $x = 4096$	M1A1 [7]	
	Tota	al 7 marks	

NOTE WELL! This can be solved using a modern calculator. No working = no marks. Award marks only for work explicitly seen.

Mark	Notes		
Works	Works in base 4		
M1	For changing the base of the log correctly to base 4		
	$3\log_4 x + 8\log_x 64 = 22 \Rightarrow 3\log_4 x + \frac{8\log_4 4^3}{\log_4 x} = 22$		
M1	For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_4 64 = 3\log_4 4$		
M1	For multiplying through by $\log_4 x$ and forming a 3TQ in log base 4		
M1	For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 They must obtain two values for their log.		
A1	For both correct values of $\log x \left[\frac{4}{3}, 6 \right]$		
M1	For undoing either log correctly. Allow this mark for any erroneous log they find, but undo correctly.		
A1	For both values of x Accept $4^{\frac{4}{3}}$ or awrt 6.35 and 4^{6} or 4096		

Works in base x		App.	
M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrectly, but they must obtain a value for $x =$. A1 For applying their 3TQ by any varied by they find, but undo correctly. A1 For both correct values. A1 For providing their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 A1 For both correct values. A2 For both correct values. A3 For both correct values. A4 For both correct values, log _x $4 = \frac{3}{4}, \frac{1}{6}$ M1 For undoing either log correctly, but they must obtain a value for $x =$ A2 For both correct values, log _x $4 = \frac{3}{4}, \frac{1}{6}$ M1 For undoing either log correctly, but they must obtain a value for $x =$ A2 A1 Accept 4^3 or $x = 4^6$ Allow this mark for any erroneous log they find, but undo correctly. A1 Accept 4^3 or awrt 6.35 and 4^6 or 4096 Works in base 2 M1 Changes the base of at least one log to base 2. $\frac{3}{2} \log_2 x$, $\frac{8 \log_3 x^6}{\log_2 x}$ M1 For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_2 64 = 6\log_2 2$ M1 For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 (12log ₂ $x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =$, A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = \frac{2^3}{3}$ or $x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.			3
M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrectly, but they must obtain a value for $x =$. A1 For applying their 3TQ by any varied by they find, but undo correctly. A1 For both correct values. A1 For providing their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 A1 For both correct values. A2 For both correct values. A3 For both correct values. A4 For both correct values, log _x $4 = \frac{3}{4}, \frac{1}{6}$ M1 For undoing either log correctly, but they must obtain a value for $x =$ A2 For both correct values, log _x $4 = \frac{3}{4}, \frac{1}{6}$ M1 For undoing either log correctly, but they must obtain a value for $x =$ A2 A1 Accept 4^3 or $x = 4^6$ Allow this mark for any erroneous log they find, but undo correctly. A1 Accept 4^3 or awrt 6.35 and 4^6 or 4096 Works in base 2 M1 Changes the base of at least one log to base 2. $\frac{3}{2} \log_2 x$, $\frac{8 \log_3 x^6}{\log_2 x}$ M1 For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_2 64 = 6\log_2 2$ M1 For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 (12log ₂ $x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =$, A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = \frac{2^3}{3}$ or $x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.	***	• 1 · · · ·	Studentre
M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrectly, but they must obtain a value for $x =$. A1 For applying their 3TQ by any varied by they find, but undo correctly. A1 For both correct values. A1 For providing their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 A1 For both correct values. A2 For both correct values. A3 For both correct values. A4 For both correct values, log _x $4 = \frac{3}{4}, \frac{1}{6}$ M1 For undoing either log correctly, but they must obtain a value for $x =$ A2 For both correct values, log _x $4 = \frac{3}{4}, \frac{1}{6}$ M1 For undoing either log correctly, but they must obtain a value for $x =$ A2 A1 Accept 4^3 or $x = 4^6$ Allow this mark for any erroneous log they find, but undo correctly. A1 Accept 4^3 or awrt 6.35 and 4^6 or 4096 Works in base 2 M1 Changes the base of at least one log to base 2. $\frac{3}{2} \log_2 x$, $\frac{8 \log_3 x^6}{\log_2 x}$ M1 For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_2 64 = 6\log_2 2$ M1 For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 (12log ₂ $x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =$, A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = \frac{2^3}{3}$ or $x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.		In base x	On. C
M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrectly, but they must obtain a value for $x =$. A1 For applying their 3TQ by any varied by they find, but undo correctly. A1 For both correct values. A1 For providing their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 A1 For both correct values. A2 For both correct values. A3 For both correct values. A4 For both correct values, log _x $4 = \frac{3}{4}, \frac{1}{6}$ M1 For undoing either log correctly, but they must obtain a value for $x =$ A2 For both correct values, log _x $4 = \frac{3}{4}, \frac{1}{6}$ M1 For undoing either log correctly, but they must obtain a value for $x =$ A2 A1 Accept 4^3 or $x = 4^6$ Allow this mark for any erroneous log they find, but undo correctly. A1 Accept 4^3 or awrt 6.35 and 4^6 or 4096 Works in base 2 M1 Changes the base of at least one log to base 2. $\frac{3}{2} \log_2 x$, $\frac{8 \log_3 x^6}{\log_2 x}$ M1 For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_2 64 = 6\log_2 2$ M1 For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 (12log ₂ $x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =$, A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = \frac{2^3}{3}$ or $x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.	IVII	For changing the base of the log correctly to base x of vice versa.	ON
This mark can also be awarded for explicit application of the power law on $\log_x 64 = 3\log_x 4$ M1 For multiplying through by $\log_x 4$ and forming a 3TQ in $\log base x$ $\frac{3}{\log_x 4} + 24\log_x 4 = 22 \Rightarrow 24(\log_x 4)^2 - 22\log_x 4 + 3 = 0$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $24(\log_x 4)^2 - 22\log_x 4 + 3 = 0 \Rightarrow (4\log_x 4 - 3)(6\log_x 4 - 1) = 0 \Rightarrow \log_x 4 =,$ They must obtain two values for their \log . A1 For both correct values. $\log_x 4 = \frac{3}{4}, \frac{1}{6}$ M1 For undoing either \log correctly, but they must obtain a value for $x =$ $x = \frac{4^3}{3} \text{ or } x = 4^6$ Allow this mark for any erroneous \log they find, but undo correctly. A1 $\frac{4}{3}$ Accept $\frac{4^3}{3}$ or awrt 6.35 and $\frac{4^6}{3}$ or 4096 Works in base 2 M1 Changes the base of at least one \log to base 2. $\frac{3}{2}\log_2 x$, $\frac{8\log_x x^6}{\log_2 x}$ M1 For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_x 64 = 6\log_x 2$ M1 For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either \log correctly. $x = 2^{\frac{8}{3}} \text{ or } x = 2^{12}$ Allow this mark for any erroneous \log they find, but undo correctly.		$\log_4 x^3 + 8\log_x 64 = 22 \Rightarrow \frac{8\log_x x}{\log_x 4} + 8\log_x 4^3 = 22$	
log _x 64 = 3 log _x 4 M1 For multiplying through by log _x 4 and forming a 3TQ in log base x $\frac{3}{\log_x 4} + 24 \log_x 4 = 22 \Rightarrow 24(\log_x 4)^2 - 22 \log_x 4 + 3 = 0$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $24(\log_x 4)^2 - 22 \log_x 4 + 3 = 0 \Rightarrow (4\log_x 4 - 3)(6\log_x 4 - 1) = 0 \Rightarrow \log_x 4 =,$ They must obtain two values for their log _x . A1 For both correct values. $\log_x 4 = \frac{3}{4}, \frac{1}{6}$ M1 For undoing either log correctly, but they must obtain a value for $x =$ $x = \frac{4^3}{3}$ or $x = 4^6$ Allow this mark for any erroneous log they find, but undo correctly. A1 Accept 4^3 or awrt 6.35 and 4^6 or 4096 Works in base 2 M1 Changes the base of at least one log to base 2. $\frac{3}{2} \log_2 x$, $\frac{8 \log_x x^6}{\log_2 x}$ M1 For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_2 64 = 6\log_2 2$ M1 For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $\frac{8}{x} = 2^3$ or $x = 2^1$ Allow this mark for any erroneous log they find, but undo correctly.	M1		
M1 For multiplying through by $\log_x 4$ and forming a 3TQ in log base x $\frac{3}{\log_x 4} + 24 \log_x 4 = 22 \Rightarrow 24 (\log_x 4)^2 - 22 \log_x 4 + 3 = 0$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $24 (\log_x 4)^2 - 22 \log_x 4 + 3 = 0 \Rightarrow (4 \log_x 4 - 3)(6 \log_x 4 - 1) = 0 \Rightarrow \log_x 4 =,$ They must obtain two values for their $\log_x 4 = \frac{3}{4}, \frac{1}{6}$ M1 For undoing either $\log_x 4 = \frac{3}{4}, \frac{1}{6}$ M1 For undoing either log correctly, but they must obtain a value for $x =$ $x = \frac{4}{3} \text{ or } x = 4^6$ Allow this mark for any erroneous $\log_x 4 = \frac{3}{4}, \frac{1}{6}$ Works in base 2 M1 Changes the base of at least one $\log_x 4 = \frac{3}{2} \log_2 x, \frac{8 \log_x x^6}{\log_2 x}$ M1 For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_x 64 = 6\log_x 2$ M1 For multiplying through by $\log_x x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22 \log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44 \log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 (12 $\log_x x - 1)(8 \log_x x - 3) = 0 \Rightarrow \log_x x =,$ A1 For both correct values. $\log_x x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $\frac{8}{x = 2^3} \text{ or } x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.			
$\frac{3}{\log_x 4} + 24\log_x 4 = 22 \Rightarrow 24(\log_x 4)^2 - 22\log_x 4 + 3 = 0$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $24(\log_x 4)^2 - 22\log_x 4 + 3 = 0 \Rightarrow (4\log_x 4 - 3)(6\log_x 4 - 1) = 0 \Rightarrow \log_x 4 =,$ They must obtain two values for their log. A1 For both correct values. $\log_x 4 = \frac{3}{4}, \frac{1}{6}$ M1 For undoing either log correctly, but they must obtain a value for $x =$ $x = 4^{\frac{1}{3}} \text{ or } x = 4^{6}$ Allow this mark for any erroneous log they find, but undo correctly. A1 Accept $4^{\frac{4}{3}}$ or awrt 6.35 and 4^{6} or 4096 Works in base 2 M1 Changes the base of at least one log to base 2. $\frac{3}{2}\log_2 x$, $\frac{8\log_x x^6}{\log_2 x}$ M1 For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_2 64 = 6\log_2 2$ M1 For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 (12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow 10g_2 x =, A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $\frac{8}{x} = 2^{\frac{1}{3}} \text{ or } x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.			
M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $24(\log_x 4)^2 - 22\log_x 4 + 3 = 0 \Rightarrow (4\log_x 4 - 3)(6\log_x 4 - 1) = 0 \Rightarrow \log_x 4 =,$ They must obtain two values for their log. A1 For both correct values. $\log_x 4 = \frac{3}{4}, \frac{1}{6}$ M1 For undoing either log correctly, but they must obtain a value for $x =$ $x = 4^{\frac{1}{3}}$ or $x = 4^{6}$ Allow this mark for any erroneous log they find, but undo correctly. A1 Accept $4^{\frac{1}{3}}$ or awrt 6.35 and 4^{6} or 4096 Works in base 2 M1 Changes the base of at least one log to base 2. $\frac{3}{2}\log_2 x$, $\frac{8\log_x x^6}{\log_2 x}$ M1 For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_2 64 = 6\log_2 2$ M1 For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $\frac{8}{x} = 2^{\frac{1}{3}}$ or $x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.	M1	For multiplying through by $\log_x 4$ and forming a 3TQ in log base x	
If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $24(\log_x 4)^2 - 22\log_x 4 + 3 = 0 \Rightarrow (4\log_x 4 - 3)(6\log_x 4 - 1) = 0 \Rightarrow \log_x 4 =,$ They must obtain two values for their log. A1 For both correct values. $\log_x 4 = \frac{3}{4}, \frac{1}{6}$ M1 For undoing either log correctly, but they must obtain a value for $x =$ $x = 4^{\frac{1}{3}}$ or $x = 4^6$ Allow this mark for any erroneous log they find, but undo correctly. A1 Accept $4^{\frac{1}{3}}$ or awrt 6.35 and 4^6 or 4096 Works in base 2 M1 Changes the base of at least one log to base 2. $\frac{3}{2}\log_2 x$, $\frac{8\log_x x^6}{\log_2 x}$ M1 For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_2 64 = 6\log_2 2$ M1 For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 (12\log_2 x - 1)(8\log_2 x - 3) = 0 \ightarrow \log_2 x = \frac{8}{3}, 12 M1 For undoing either $\log_2 x = 0$ and $\log_2 x = 0$ an		$\frac{3}{\log_x 4} + 24\log_x 4 = 22 \Rightarrow 24(\log_x 4)^2 - 22\log_x 4 + 3 = 0$	
following a correct 3TQ this is M0 $24(\log_x 4)^2 - 22\log_x 4 + 3 = 0 \Rightarrow (4\log_x 4 - 3)(6\log_x 4 - 1) = 0 \Rightarrow \log_x 4 =,$ They must obtain two values for their log. A1 For both correct values. $\log_x 4 = \frac{3}{4}, \frac{1}{6}$ M1 For undoing either log correctly, but they must obtain a value for $x =$. $x = 4^{\frac{1}{3}} \text{ or } x = 4^{6}$ Allow this mark for any erroneous log they find, but undo correctly. A1 Accept $4^{\frac{1}{3}}$ or awrt 6.35 and 4^{6} or 4096 Works in base 2 M1 Changes the base of at least one log to base 2. $\frac{3}{2}\log_2 x, \frac{8\log_x x^6}{\log_2 x}$ M1 For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_2 64 = 6\log_2 2$ M1 For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = 2^{\frac{3}{3}} \text{ or } x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.	M1		
They must obtain two values for their log. A1 For both correct values. $\log_x 4 = \frac{3}{4}, \frac{1}{6}$ M1 For undoing either log correctly, but they must obtain a value for $x = \dots$		following a correct 3TQ this is M0	
A1 For both correct values. $\log_x 4 = \frac{3}{4}, \frac{1}{6}$ M1 For undoing either log correctly, but they must obtain a value for $x =$ $x = 4^{\frac{1}{3}}$ or $x = 4^{6}$ Allow this mark for any erroneous log they find, but undo correctly. A1 Accept $4^{\frac{1}{3}}$ or awrt 6.35 and 4^{6} or 4096 Works in base 2 M1 Changes the base of at least one log to base 2. $\frac{3}{2}\log_2 x$, $\frac{8\log_x x^6}{\log_2 x}$ M1 For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_2 64 = 6\log_2 2$ M1 For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = \frac{8}{2^{\frac{3}{3}}} \text{ or } x = 2^{12}$ Allow this for any erroneous log they find, but undo correctly.		$24(\log_x 4)^2 - 22\log_x 4 + 3 = 0 \Rightarrow (4\log_x 4 - 3)(6\log_x 4 - 1) = 0 \Rightarrow \log_x 4 =,$	
M1 For undoing either log correctly, but they must obtain a value for $x =$ $x = 4^{\frac{4}{3}} \text{ or } x = 4^{6}$ Allow this mark for any erroneous log they find, but undo correctly. A1 Accept $4^{\frac{4}{3}}$ or awrt 6.35 and 4^{6} or 4096 Works in base 2 M1 Changes the base of at least one log to base 2. $\frac{3}{2} \log_{2} x$, $\frac{8 \log_{x} x^{6}}{\log_{2} x}$ M1 For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_{2} 64 = 6 \log_{2} 2$ M1 For multiplying through by $\log_{2} x$ and forming a 3TQ in base 2 $\frac{3}{2} (\log_{2} x)^{2} - 22 \log_{2} x + 48 = 0 \Rightarrow \left[3(\log_{2} x)^{2} - 44 \log_{2} x + 96 = 0 \right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $(12 \log_{2} x - 1)(8 \log_{2} x - 3) = 0 \Rightarrow \log_{2} x =,$ A1 For both correct values. $\log_{2} x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = 2^{\frac{8}{3}} \text{ or } x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.			
Allow thank for any erroneous log they find, but undo correctly. Allow thank for any erroneous log they find, but undo correctly. Allow thank for any erroneous log they find, but undo correctly. Accept $4^{\frac{4}{3}}$ or awrt 6.35 and 4^{6} or 4096 Works in base 2 M1 Changes the base of at least one log to base 2. $\frac{3}{2} \log_2 x$, $\frac{8\log_x x^6}{\log_2 x}$ M1 For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_2 64 = 6\log_2 2$ M1 For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = 2^{\frac{8}{3}}$ or $x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.	A1	For both correct values. $\log_x 4 = \frac{3}{4}, \frac{1}{6}$	
Allow this mark for any erroneous log they find, but undo correctly. A1 $\frac{4}{3}$ or awrt 6.35 and 4^6 or 4096 Works in base 2 M1 Changes the base of at least one log to base 2. $\frac{3}{2} \log_2 x$, $\frac{8 \log_x x^6}{\log_2 x}$ M1 For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_2 64 = 6\log_2 2$ M1 For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = 2^{\frac{8}{3}}$ or $x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.	M1	For undoing either log correctly, but they must obtain a value for $x = \dots$	
Allow this mark for any erroneous log they find, but undo correctly. A1 $\frac{4}{3}$ or awrt 6.35 and 4^6 or 4096 Works in base 2 M1 Changes the base of at least one log to base 2. $\frac{3}{2} \log_2 x$, $\frac{8 \log_x x^6}{\log_2 x}$ M1 For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_2 64 = 6\log_2 2$ M1 For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = 2^{\frac{8}{3}}$ or $x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.		$x = 4\frac{4}{3}$ or $x = 46$	
A1Accept $4^{\frac{4}{3}}$ or awrt 6.35 and 4^6 or 4096Works in base 2M1Changes the base of at least one log to base 2. $\frac{3}{2} \log_2 x$, $\frac{8 \log_x x^6}{\log_2 x}$ M1For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_2 64 = 6\log_2 2$ M1For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1For both correct values. $\log_2 x = \frac{8}{3}$, 12M1For undoing either log correctly. $x = 2^{\frac{12}{3}}$ or $x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.			
Works in base 2M1Changes the base of at least one log to base 2. $\frac{3}{2} \log_2 x$, $\frac{8 \log_x x^6}{\log_2 x}$ M1For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_2 64 = 6\log_2 2$ M1For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1For both correct values. $\log_2 x = \frac{8}{3}$, 12M1For undoing either log correctly. $x = 2^{\frac{8}{3}}$ or $x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.	A1	4	
M1 Changes the base of at least one log to base 2. $\frac{3}{2}\log_2 x$, $\frac{8\log_x x^6}{\log_2 x}$ M1 For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_2 64 = 6\log_2 2$ M1 For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = 2^{\frac{8}{3}}$ or $x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.		1	
Changes the base of at least one log to base 2. $\frac{1}{2} \log_2 x$, $\frac{3\log_2 x}{\log_2 x}$ M1 For applying the power law correctly seen anywhere in their work. This mark can also be awarded for explicit application of the power law on $\log_2 64 = 6\log_2 2$ M1 For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = 2^{\frac{8}{3}} \text{ or } x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.			
This mark can also be awarded for explicit application of the power law on $\log_2 64 = 6\log_2 2$ M1 For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = 2^{\frac{8}{3}} \text{ or } x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.	MI	Changes the base of at least one log to base 2. $\frac{3}{2}\log_2 x$, $\frac{8\log_x x^6}{\log_2 x}$	
M1 For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = 2^{\frac{8}{3}} \text{ or } x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.	M1		
M1 For multiplying through by $\log_2 x$ and forming a 3TQ in base 2 $\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = 2^{\frac{8}{3}} \text{ or } x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.			
$\frac{3}{2}(\log_2 x)^2 - 22\log_2 x + 48 = 0 \Rightarrow \left[3(\log_2 x)^2 - 44\log_2 x + 96 = 0\right]$ M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = 2^{\frac{8}{3}} \text{ or } x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.			
M1 For solving their 3TQ by any valid and correct method. If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = 2^{\frac{8}{3}}$ or $x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.	M1		
If there is no method seen with an incorrect 3TQ or with incorrect solutions following a correct 3TQ this is M0 $(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = 2^{\frac{8}{3}}$ or $x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.			
following a correct 3TQ this is M0 $(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = 2^{\frac{8}{3}} \text{ or } x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.	M1		
$(12\log_2 x - 1)(8\log_2 x - 3) = 0 \Rightarrow \log_2 x =,$ A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = 2^{\frac{8}{3}} \text{ or } x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.			
A1 For both correct values. $\log_2 x = \frac{8}{3}$, 12 M1 For undoing either log correctly. $x = 2^{\frac{8}{3}}$ or $x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.			
M1 For undoing either log correctly. $x = 2^{\frac{8}{3}}$ or $x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.	A 1	$(12\log_2 x - 1)(\log_2 x - 3) - 0 \rightarrow \log_2 x - \dots, \dots$	
$x = 2^{\frac{8}{3}} \text{ or } x = 2^{12}$ Allow this mark for any erroneous log they find, but undo correctly.	Al		
Allow this mark for any erroneous log they find, but undo correctly.	M1	8	
Allow this mark for any erroneous log they find, but undo correctly.		$x = 2^{\frac{6}{3}}$ or $x = 2^{12}$	
Δ1 8			
	A1	8	

		thos:
		Trishstude
Question	Scheme	Marks
11(a)	$\cos 2A = \cos^2 A - \sin^2 A \Rightarrow \cos 2A = \left(1 - \sin^2 A\right) - \sin^2 A = 1 - 2\sin^2 A$	M1M1
	$2\sin^2 A = 1 - \cos 2A \Rightarrow \sin^2 A = \frac{1}{2}(1 - \cos 2A) *$	A1cso [3]
(b)	$\cos^2 A = \frac{1}{2} \left(1 + \cos 2A \right)$	B1
	$\sin^4 x + \cos^4 x = \left(\left(\frac{1 - \cos 2x}{2} \right)^2 + \left(\frac{1 + \cos 2x}{2} \right)^2 \right)$	
	$= \frac{1}{4} \left(\left(1 - \cos 2x \right)^2 + \left(1 + \cos 2x \right)^2 \right)$	
	$= \frac{1}{4} \left(1 - 2\cos 2x + \cos^2 2x + 1 + 2\cos 2x + \cos^2 2x \right)$	M1
	$= \frac{1}{4} (2 + 2\cos^2 2x) = \left\{ \frac{1}{2} (1 + \cos^2 2x) \right\}$	A1
	$\left\{\cos^2 2x = \frac{1 + \cos 4x}{2}\right\}$	M1A1
	$\sin^4 x + \cos^4 x = \frac{1}{2} \left(1 + \frac{1 + \cos 4x}{2} \right) = \frac{3 + \cos 4x}{4} $	cso [5]
(c)	$5\sin 2\theta + 6 = 8\left(\frac{3+\cos 2\theta}{4}\right) \Rightarrow 5\sin 2\theta + 6 = 6+2\cos 2\theta$	M1
	$\Rightarrow 5\sin 2\theta = 2\cos 2\theta \Rightarrow \frac{\sin 2\theta}{\cos 2\theta} = \frac{2}{5} \Rightarrow \tan 2\theta = \frac{2}{5}$	M1
	$2\theta = 21.801^{\circ}, 201.801^{\circ}, 381.801^{\circ}$	A1
	$\Rightarrow \theta = 10.9^{\circ}, 100.9^{\circ}$	A1 [4]
	Penalise extra angles in range by withholding the final A mark. Extra angles out of range – ignore.	
		otal 12 marks

Part	Mark	Notes
(a)	M1	For using the summation formula for cos 2A
		They must start with either
		$\cos 2A = \cos^2 A - \sin^2 A \text{or} \cos (A + A) = \cos A \cos A - \sin A \sin A$
	M1	For eliminating $\cos^2 A$ using $\cos^2 A + \sin^2 A = 1$ and attempting to rearrange to the required result. This is not dependent on the first M mark, so if they start with another identity for $\cos 2A$ they can still get this mark.
	A1	For the correct identity with no errors seen.
	cso	This is a given result.
	NB Sor	ne candidates work backwards – that is fine, please follow their working.

Working with a different variable.

https://britishstudentroom.com/ If they work in this part with a different variable (eg A) then award all the marks as appropriate up to the last mark.

If they leave their final answer in terms of another variable, withhold the final A mark

If they however, change to x on the final line award all the marks [provided everything

is corr	rect]		
(b)	Main n	nethod	
	B1	For use of the correct identity for $\cos^2 x$	
		$\left[\cos^2 x = \frac{1}{2}(1 + \cos 2x)\right] \text{ or if they convert } \cos^2 x \text{ to } \sin^2 x \text{ use the}$	
		Pythagorean identity $\cos^2 x = 1 - \sin^2 x$ and apply the given identity.	
	M1	For squaring both identities. This must be a correct expansion.	
		Ft their identity for $\left[\cos^2 x = \frac{1}{2}(1+\cos 2x)\right]$	
	A1	For collecting like terms and obtaining $\frac{1}{2}(1+\cos^2 2x)$ oe.	
		For example, $\frac{1}{4} \left(2 + 2\cos^2 2x \right)$	
	M1	For applying the identity:	
		$\cos^2 A = \frac{1}{2}(1 + \cos 2A) \Rightarrow \left[\cos^2 2A = \frac{1}{2}(1 + \cos 4A)\right]$	
		on $\cos^2 2x$ only again to achieve an expression in $\cos 4x$ only	
	A1	For the correct identity with no errors seen.	
	cso	This is a given result. You must check every line of their work carefully.	
	ALT 1	carefully.	
	B1	For use of the correct identity for $\sin 2A = 2\sin A\cos A$ [seen later in	
		their working].	
	M1	For using the expansion of $\sin^2 x + \cos^2 x$ as follows	
		$\sin^4 x + \cos^4 x = \left(\sin^2 x + \cos^2 x\right)^2 - 2\sin^2 x \cos^2 x$	
		This must be correct	
	A1	For obtaining $\sin^4 x + \cos^4 x = 1 - \frac{1}{2}\sin^2 2x$ oe.	
		For example; $\frac{1}{2}(2-\sin^2 2x)$	
	M1	For applying the given identity on $\sin^2 2x$ only to achieve an expression in $\cos 4x$ only	
		$\sin^2 A = \frac{1}{2} (1 - \cos 2A) \Rightarrow \left[\sin^2 2A = \frac{1}{2} (1 - \cos 4A) \right]$	
		$\sin^4 x + \cos^4 x = 1 - \frac{1}{2} \left(\frac{1 - \cos 4x}{2} \right) \Rightarrow \left(\sin^4 x + \cos^4 x = \frac{3 + \cos 4x}{4} \right)$	
	A1	For the correct identity with no errors seen.	
	cso	This is a given result. You must check every line of their work	
		carefully.	

	hr _{tbs://h}	
	— Works backwards from the given result	Studentre
AIT 2	– Works backwards from the given result	On.C
B1	For use of the correct identity for $\sin 2A = 2\sin A\cos A$ [seen later in their working].	
M1	Applies the cos2A identity and converts 3 into $3(\sin^2 2x + \cos^2 2x)$ $\frac{3 + \cos 4x}{4} = \frac{3\sin^2 2x + 3\cos^2 2x + (\cos^2 2x - \sin^2 2x)}{4}$	
A1	Obtains $\frac{3 + \cos 4x}{4} = \frac{4\cos^2 2x + 2\sin^2 2x}{4}$	
M1	Applies the cos2A identity and expands the bracket. $\frac{3 + \cos 4x}{4} = \frac{4\left(\cos^2 x - \sin^2 x\right)^2 + 8\sin^2 x \cos^2 x}{4}$ $= \frac{4\cos^4 x - 8\sin^2 x \cos^2 x + 4\sin^4 x + 8\sin^2 x \cos^2 x}{4}$	
A1 cso	Simplifies to the required result with no errors seen $\frac{3 + \cos 4x}{4} = \sin^4 x + \cos^4 x *$	

(c)	M1	For obtaining the correct equation in terms of $\sin 2\theta$ and $\cos 2\theta$
		$6 + 2\cos 2\theta = 5\sin 2\theta + 6$
		Accept unsimplified, accept even: $8\left(\frac{3+\cos 2\theta}{4}\right) = 5\sin 2\theta + 6$
	M1	For using the $\tan 2\theta = \frac{\sin 2\theta}{\cos 2\theta}$ identity correctly on their expression
		following an expression in the form $A\cos 2\theta = B\sin 2\theta$ and must be in terms of 2θ
	A1	For achieving at least one correct angle for 2θ
		NB This is an M mark in Epen
	A1	For awrt both 10.9° and 100.9°
		Penalise extra angles in range by withholding the final A mark.
		Extra angles out of range – ignore.

hribs: Joritishshidentroom.com/

Pearson Education Limited. Registered company number 872828 with its registered office at 80 Strand, London, WC2R 0RL, United Kingdom