

Please check the examination details below before entering your candidate information

Candidate surname

Other names

Centre Number

Candidate Number

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**Pearson Edexcel International GCSE**

Time 2 hours

Paper  
reference

**4PM1/02R**

**Further Pure Mathematics**  
**PAPER 2R**



**Calculators may be used.**

Total Marks

## Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You must **NOT** write anything on the formulae page.  
Anything you write on the formulae page will gain NO credit.

## Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

## Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ►

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Pearson

**Mensuration**

Surface area of sphere =  $4\pi r^2$

Curved surface area of cone =  $\pi r \times$  slant height

Volume of sphere =  $\frac{4}{3}\pi r^3$

**Series**

**Arithmetic series**

Sum to  $n$  terms,  $S_n = \frac{n}{2}[2a + (n - 1)d]$

**Geometric series**

Sum to  $n$  terms,  $S_n = \frac{a(1 - r^n)}{(1 - r)}$

Sum to infinity,  $S_\infty = \frac{a}{1 - r}$   $|r| < 1$

**Binomial series**

$(1 + x)^n = 1 + nx + \frac{n(n - 1)}{2!}x^2 + \dots + \frac{n(n - 1)\dots(n - r + 1)}{r!}x^r + \dots$  for  $|x| < 1, n \in \mathbb{Q}$

**Calculus**

**Quotient rule (differentiation)**

$$\frac{d}{dx} \left( \frac{f(x)}{g(x)} \right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

**Trigonometry**

**Cosine rule**

In triangle  $ABC$ :  $a^2 = b^2 + c^2 - 2bc \cos A$

$\tan \theta = \frac{\sin \theta}{\cos \theta}$

$\sin(A + B) = \sin A \cos B + \cos A \sin B$

$\sin(A - B) = \sin A \cos B - \cos A \sin B$

$\cos(A + B) = \cos A \cos B - \sin A \sin B$

$\cos(A - B) = \cos A \cos B + \sin A \sin B$

$\tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$

$\tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$

**Logarithms**

$\log_a x = \frac{\log_b x}{\log_b a}$



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Answer all ELEVEN questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

1 Find the set of values for  $x$  for which

(a)  $5x - 10 > 4x - 7$  (1)

(b)  $2x^2 - 11x + 5 < 0$  (3)

(c) both  $5x - 10 > 4x - 7$  and  $2x^2 - 11x + 5 < 0$  (1)

Dotted lines for working.

(Total for Question 1 is 5 marks)



2 The point  $A$  has coordinates  $(-7, -1)$  and the point  $B$  has coordinates  $(3, 4)$

- (a) Find an equation of the line that passes through  $A$  and  $B$   
Give your answer in the form  $ax + by + c = 0$  where  $a$ ,  $b$  and  $c$  are integers.

(3)

The point  $C$  has coordinates  $(-3, 7)$

Given that  $k$  is a constant such that  $AB = kAC$

- (b) find the value of  $k$

(2)

The point  $D$  has coordinates  $(3, p)$  where  $p$  is a constant.

Given that  $CD$  is perpendicular to  $AB$

- (c) find the value of  $p$

(3)

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**Question 2 continued**

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**(Total for Question 2 is 8 marks)**



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3 Differentiate with respect to  $x$

(a)  $e^{2x} \sqrt{5x - 3}$

(3)

(b)  $\frac{x^3}{\cos 3x}$

(3)

Handwriting practice area with 20 horizontal dotted lines.



**Question 3 continued**

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**(Total for Question 3 is 6 marks)**



4 The quadratic equation

$$2x^2 + 4x + 3 = 0$$

has roots  $\alpha$  and  $\beta$

(a) Without solving the equation, show that  $\alpha^2 + \beta^2 = 1$  (4)

(b) Without solving the equation, find the value of  $\alpha^4 + \beta^4$  (3)

(c) Hence form a quadratic equation with integer coefficients that has roots  $\alpha^4$  and  $\beta^4$  (3)

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### Question 4 continued

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Question 4 continued

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**Question 4 continued**

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**(Total for Question 4 is 10 marks)**



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### Question 5 continued

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Question 5 continued

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**Question 5 continued**

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**(Total for Question 5 is 10 marks)**



6 The curve  $C$  has equation

$$y = 4\sqrt{x}$$

The point  $A$  on  $C$  has coordinates  $(9, 12)$

The tangent to  $C$  at the point  $A$  meets the  $x$ -axis at the point  $T$

(a) Find the coordinates of  $T$  (5)

The normal to  $C$  at the point  $A$  meets the  $x$ -axis at the point  $N$

(b) Find the coordinates of  $N$  (4)

(c) Calculate the area of triangle  $ATN$  (2)

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**Question 6 continued**

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**(Total for Question 6 is 11 marks)**





**Question 7 continued**

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Handwriting practice area consisting of 25 horizontal dotted lines.

**(Total for Question 7 is 8 marks)**



8 Liquid drips onto a large horizontal flat cloth, forming a circular stain.

The liquid starts to drip onto the cloth at time  $t = 0$

The area of the stain increases at a constant rate of  $1.5 \text{ cm}^2/\text{s}$

(a) Find, in terms of  $\pi$ , the radius of the stain at time  $t = 4$  seconds. (3)

(b) Find, in  $\text{cm/s}$  to 3 significant figures, the rate at which the radius of the stain is increasing at time  $t = 4$  seconds. (4)

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**Question 8 continued**

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Handwriting practice area consisting of 25 horizontal dotted lines.

**(Total for Question 8 is 7 marks)**



9 Given that  $\alpha$  is the acute angle such that  $\tan \alpha = \frac{2}{3}$

(a) find the exact value of  $\cos \alpha$

(1)

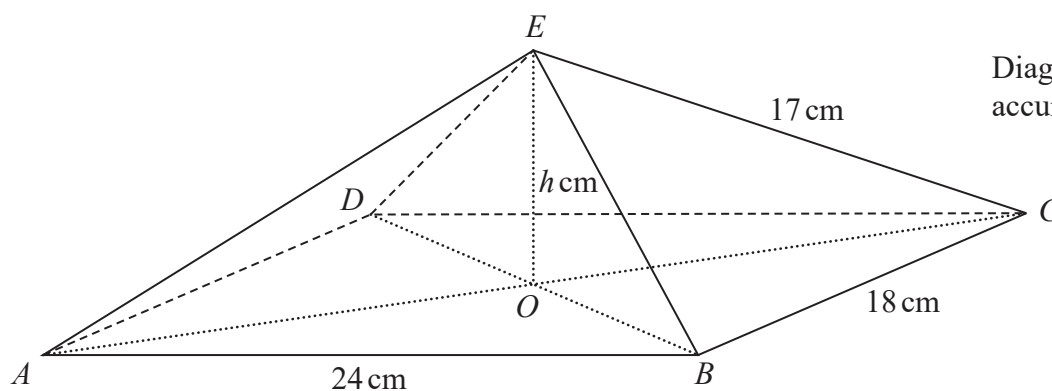


Figure 1

Figure 1 shows a right pyramid with a rectangular base  $ABCD$  and vertex  $E$

The rectangular base of the pyramid is horizontal with  $AB = 24$  cm and  $BC = 18$  cm.

The diagonals of the base intersect at the point  $O$

The vertex  $E$  of the pyramid is vertically above  $O$  such that

$$AE = BE = CE = DE = 17 \text{ cm}$$

The height of the pyramid is  $h$  cm.

(b) Find the value of  $h$

(3)

The size of the angle between the plane  $EBC$  and the plane  $ABCD$  is  $\theta^\circ$

(c) Show that  $\tan \theta^\circ = \frac{2}{3}$

(2)

The point  $P$  is the midpoint of  $EB$  and the point  $Q$  is the midpoint of  $EC$

(d) Find the size, in degrees to one decimal place, of the angle between the plane  $OPQ$  and the plane  $BCQP$

(4)

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Question 9 continued

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Question 9 continued

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**Question 9 continued**

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**(Total for Question 9 is 10 marks)**



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 Diagram NOT  
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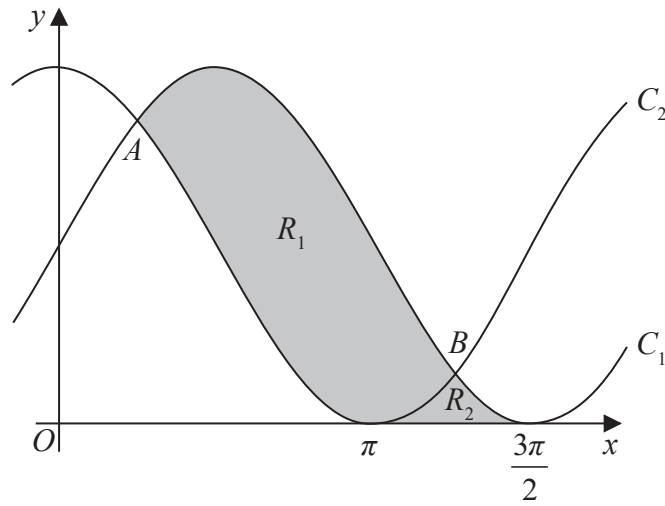


Figure 2

Figure 2 shows part of the curve  $C_1$  with equation  $y = \sin x + 1$  and part of the curve  $C_2$  with equation  $y = \cos x + 1$

As shown in Figure 2,  $C_1$  and  $C_2$  intersect at the point  $A$  and at the point  $B$

- (a) Find the exact value of the  $x$  coordinate of  $A$  and the exact value of the  $x$  coordinate of  $B$  (3)

The shaded finite region  $R_1$  shown in Figure 2 is bounded by  $C_1$  and  $C_2$

The shaded finite region  $R_2$  shown in Figure 2 is bounded by the  $x$ -axis,  $C_1$  and  $C_2$

- (b) Use calculus to find the ratio

area of  $R_1$  : area of  $R_2$

Give your answer in the form  $a : \left( \frac{\pi\sqrt{2}}{b} - c \right)$  where  $a, b$  and  $c$  are integers.

(9)

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### Question 10 continued

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Handwriting practice area with horizontal dotted lines.



Question 10 continued

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**Question 10 continued**

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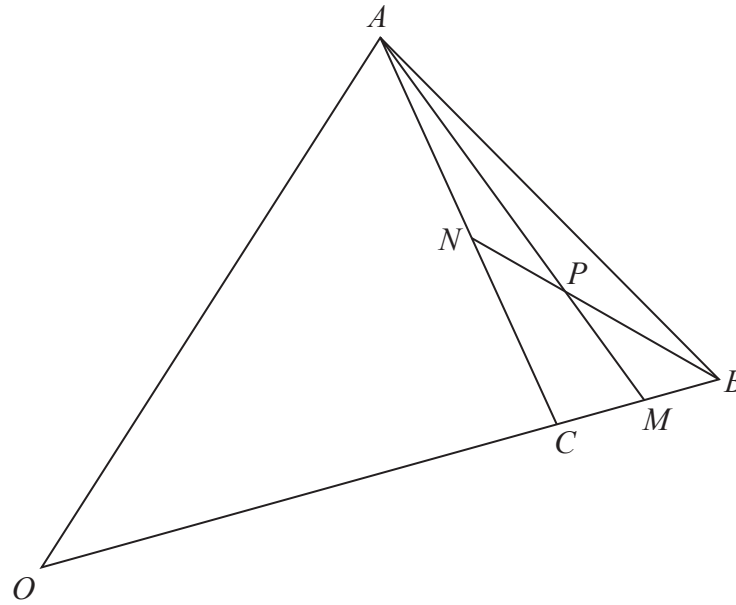
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**(Total for Question 10 is 12 marks)**



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**Figure 3**

Figure 3 shows triangle  $OAB$  with  $\vec{OA} = \mathbf{a}$  and  $\vec{OB} = \mathbf{b}$

The point  $C$  lies on  $OB$  such that  $OC:CB = 2:1$

The point  $M$  is the midpoint of  $CB$  and the point  $N$  is the midpoint of  $AC$

The lines  $AM$  and  $NB$  intersect at the point  $P$

(a) Using a vector method, find  $\vec{OP}$  as a simplified expression in terms of  $\mathbf{a}$  and  $\mathbf{b}$  (9)

The point  $Q$  is the midpoint of  $AB$

(b) Using a vector method, show that  $C, P$  and  $Q$  are collinear. (4)

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Handwriting practice area with horizontal dotted lines.



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**(Total for Question 11 is 13 marks)**

**TOTAL FOR PAPER IS 100 MARKS**

