

Please check the examination details below before entering your candidate information

Candidate surname

Other names

**Pearson  
Edexcel GCE**

Centre Number

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Candidate Number

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**Wednesday 5 June 2019**

Morning (Time: 1 hour 30 minutes)

Paper Reference **6668/01**

**Further Pure Mathematics FP2**  
**Advanced/Advanced Subsidiary**

**You must have:**

Mathematical Formulae and Statistical Tables (Pink)

Total Marks

**Candidates may use any calculator allowed by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided – *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

### Information

- The total mark for this paper is 75.
- The marks for **each** question are shown in brackets – *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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Question 2 continued

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**Question 2 continued**

Lined area for writing the answer to Question 2.

(Total 6 marks)

Q2







**Question 3 continued**

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Lined writing area for the answer to Question 3.















5. Given that

$$y \frac{d^2y}{dx^2} + 5 \left( \frac{dy}{dx} \right)^2 - 5y = 0$$

- (a) find an expression for  $\frac{d^3y}{dx^3}$  in terms of  $\frac{d^2y}{dx^2}$ ,  $\frac{dy}{dx}$  and  $y$ . **(4)**

Given also that  $y = 4$  and  $\frac{dy}{dx} = \frac{1}{2}$  at  $x = 0$

- (b) find a series solution for  $y$  in ascending powers of  $x$  with simplified coefficients, up to and including the term in  $x^3$  **(4)**

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6. (a) Show that the substitution  $v = y^{-3}$  transforms the differential equation

$$x \frac{dy}{dx} + 2y = 3x^4 y^4 \quad x > 0 \quad (\text{I})$$

into the differential equation

$$\frac{dv}{dx} - \frac{6}{x} v = -9x^3 \quad x > 0 \quad (\text{II}) \quad (5)$$

- (b) Find the general solution of the differential equation (II). (5)

- (c) Hence obtain the general solution of the differential equation (I), giving your answer in the form  $y^3 = f(x)$ . (1)

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**Question 6 continued**

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**Question 6 continued**

Area for writing the answer to Question 6 continued, consisting of 30 horizontal lines.

**Q6**

**(Total 11 marks)**

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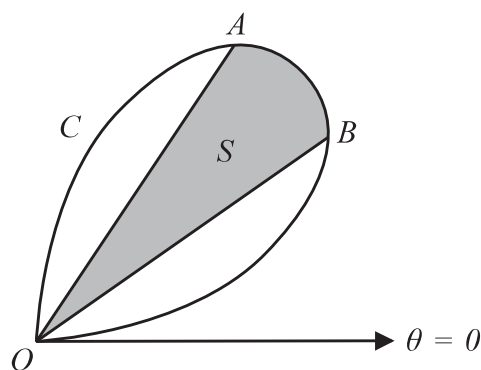


Figure 1

Figure 1 shows a curve  $C$  with polar equation

$$r = a \sin 2\theta, \quad 0 \leq \theta \leq \frac{\pi}{2}$$

where  $a$  is a positive constant.

The point  $A$  has polar coordinates  $(R, \phi)$ . The tangent to  $C$  at  $A$  is parallel to the initial line.

(a) Show that  $\tan \phi = \sqrt{2}$  (4)

(b) Find, in terms of  $a$ , the exact value of  $R$ . (2)

The tangent to  $C$  at  $B$  is perpendicular to the initial line. The region  $S$ , shown shaded in Figure 1, is bounded by  $OA$ ,  $OB$  and  $C$ , where  $O$  is the pole.

(c) Show that the area of  $S$  is given by

$$\frac{1}{2} a^2 \int_{\arctan\left(\frac{1}{\sqrt{2}}\right)}^{\arctan\sqrt{2}} \frac{1}{2} (1 - \cos 4\theta) d\theta$$
(5)

(d) Hence show that the exact area of  $S$  is

$$a^2 \left( \frac{\sqrt{2}}{18} - \frac{\pi}{8} + \frac{1}{2} \arctan \sqrt{2} \right)$$
(6)

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### Question 8 continued

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**Question 8 continued**

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**Q8**

**(Total 17 marks)**

**TOTAL FOR PAPER: 75 MARKS**

**END**

