Please check the examination de	etails below before ent	ering your candidate information		
Candidate surname		Other names		
Pearson Edexcel GCE	Centre Number	Candidate Number		
Wednesday 5 June 2019				
Morning (Time: 1 hour 30 minutes) Paper Reference 6668/01				
Further Pure Mathematics FP2 Advanced/Advanced Subsidiary				
You must have: Mathematical Formulae and St		Total Marks		

Candidates may use any calculator allowed by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use black ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
 there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information

- The total mark for this paper is 75.
- The marks for each question are shown in brackets
 use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

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$\frac{d^2}{dx}$	$\frac{y}{2} + 6\frac{\mathrm{d}y}{\mathrm{d}x} + 9y =$	$= e^{2x}$	
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	Q1
(Total 6 marks)	



Use algebra to find the set of values of x for which	
$6 \qquad x + 6$	
$\frac{6}{x-1} < \frac{x+6}{x}$	
	(6)

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Question 2 continued	



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Question 2 continued		Leav
		Q2
	(Total 6 marks)	



3. (a) Express $\frac{2}{r(r+1)(r+2)}$ in partial fractions.

(3)

(b) Hence find, in terms of n,

$$\sum_{r=1}^{n} \frac{1}{r(r+1)(r+2)} \qquad n \in \mathbb{N}, n > 1$$

Give your answer in the form $\frac{n(n+A)}{B(n+1)(n+2)}$, where A and B are constants to be found. **(4)**

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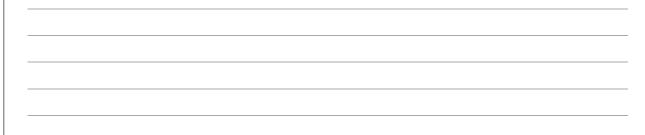
4. A transformation T from the z-plane, where z = x + iy, to the w-plane, where w = u + iv, is given by

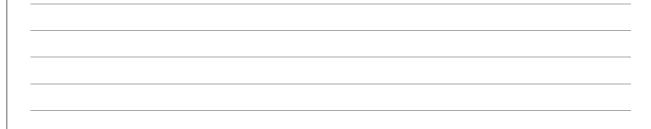
$$w=z^2+4$$

The line in the z-plane with equation y = 2 is mapped by T onto the curve C in the w-plane.

- (i) Show that C is a parabola.
- (ii) Find the coordinates of the focus of C.
- (iii) Find an equation for the directrix of C.

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Question 4 continued	



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(Total 6 marks)	



5. Given that

$$y\frac{\mathrm{d}^2 y}{\mathrm{d}x^2} + 5\left(\frac{\mathrm{d}y}{\mathrm{d}x}\right)^2 - 5y = 0$$

(a) find an expression for $\frac{d^3y}{dx^3}$ in terms of $\frac{d^2y}{dx^2}$, $\frac{dy}{dx}$ and y.

(4)

Given also that y = 4 and $\frac{dy}{dx} = \frac{1}{2}$ at x = 0

(b) find a series solution for y in ascending powers of x with simplified coefficients, up to and including the term in x^3

(4)



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Question 5 continued	



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6. (a) Show that the substitution $v = y^{-3}$ transforms the differential equation

$$x\frac{\mathrm{d}y}{\mathrm{d}x} + 2y = 3x^4y^4 \qquad x > 0 \tag{I}$$

into the differential equation

$$\frac{\mathrm{d}v}{\mathrm{d}x} - \frac{6}{x}v = -9x^3 \qquad x > 0 \tag{II}$$

(5)

(b) Find the general solution of the differential equation (II).

(5)

(c) Hence obtain the general solution of the differential equation (I), giving your answer in the form $y^3 = f(x)$.

(1)

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7. (a) Use de Moivre's theorem to show that

$$\sin 5\theta - 5\sin \theta = 16\sin^5 \theta - 20\sin^3 \theta$$

(5)

(b) Hence find the 5 distinct solutions of the equation

$$32x^5 - 40x^3 + 10x - 1 = 0$$

giving your answers to 3 decimal places where appropriate.

(5)

(c) (i) Find $\int_{C} dx$

(ii) Hence find

 $\int (8\sin^5\theta - 10\sin^3\theta) \,d\theta$ $\int_0^{\frac{\pi}{3}} (8\sin^5\theta - 10\sin^3\theta) \,d\theta$

(4)

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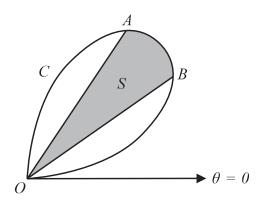


Figure 1

Figure 1 shows a curve C with polar equation

$$r = a\sin 2\theta, \quad 0 \leqslant \theta \leqslant \frac{\pi}{2}$$

where a is a positive constant.

The point A has polar coordinates (R, ϕ) . The tangent to C at A is parallel to the initial line.

(a) Show that $\tan \phi = \sqrt{2}$

(4)

(b) Find, in terms of *a*, the exact value of *R*.

(2)

The tangent to C at B is perpendicular to the initial line. The region S, shown shaded in Figure 1, is bounded by OA, OB and C, where O is the pole.

(c) Show that the area of S is given by

$$\frac{1}{2}a^2 \int_{\arctan\left(\frac{1}{\sqrt{2}}\right)}^{\arctan\sqrt{2}} \frac{1}{2} (1 - \cos 4\theta) d\theta$$
(5)

(d) Hence show that the exact area of S is

$$a^2 \left(\frac{\sqrt{2}}{18} - \frac{\pi}{8} + \frac{1}{2} \arctan \sqrt{2} \right)$$
 (6)

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	TOTAL FOR PAPER: 75 MARKS	
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